

Turbulent Flows

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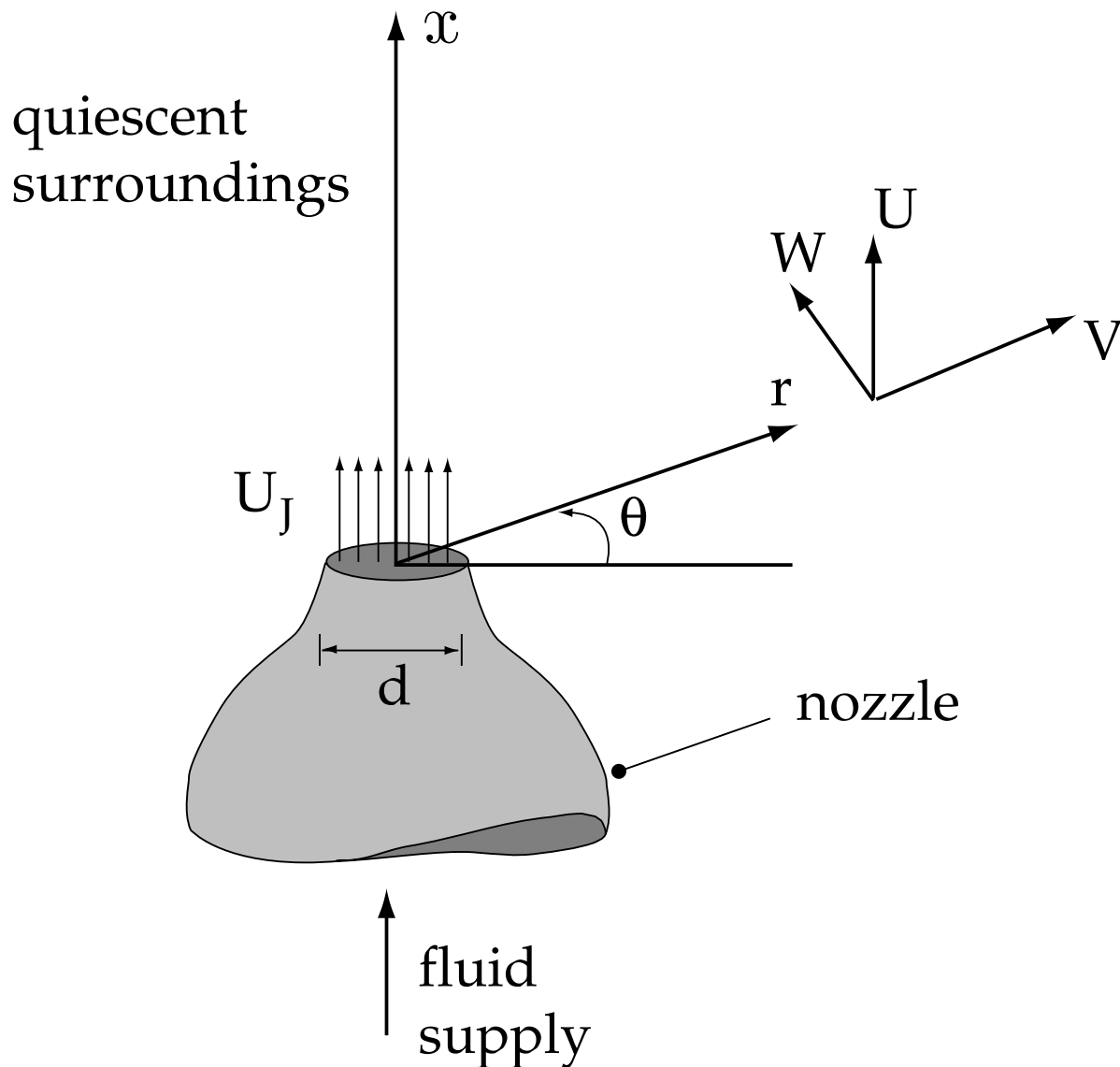


Figure 5.1: Sketch of a round jet experiment, showing the polar-cylindrical coordinate system employed.

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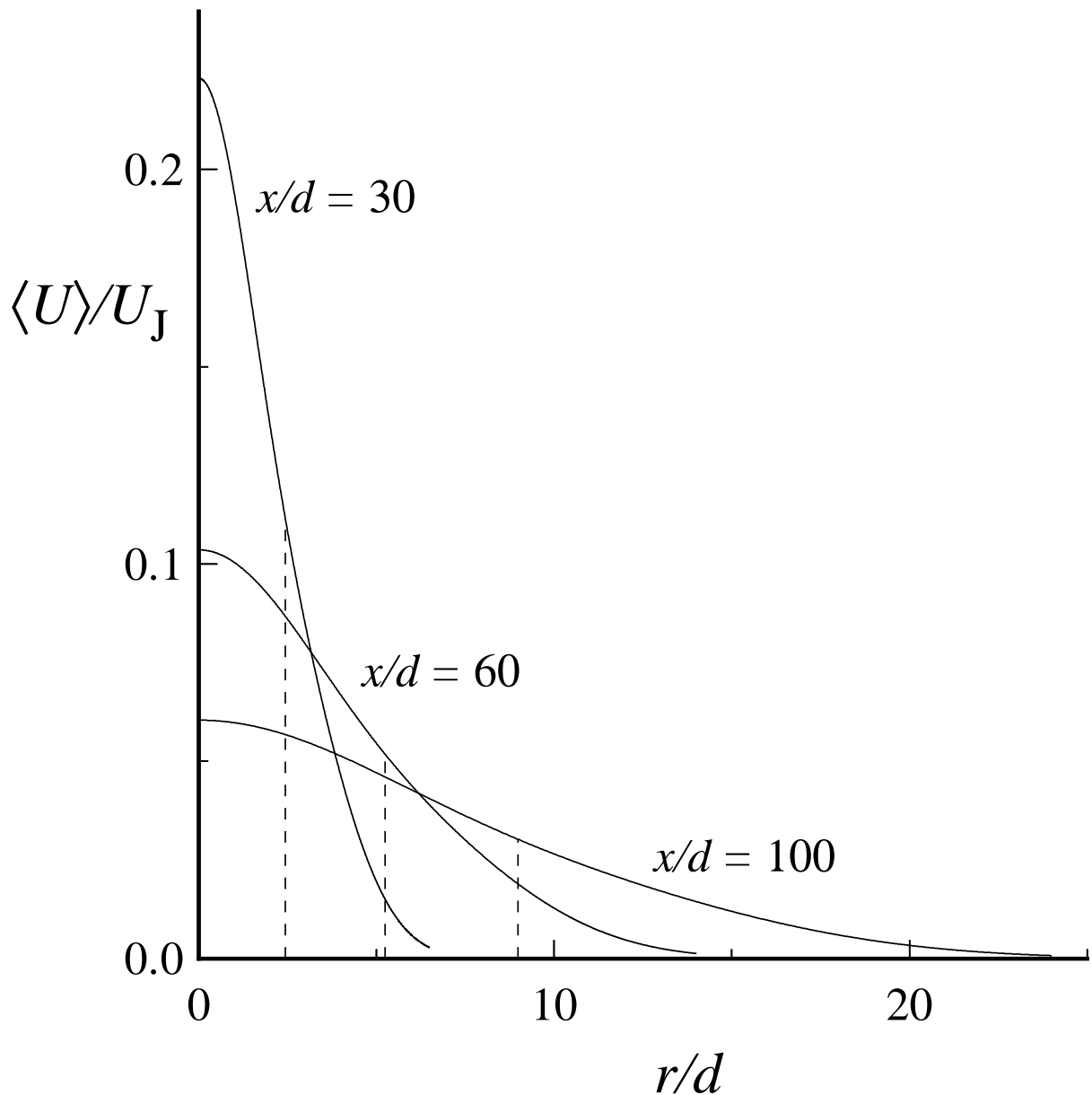


Figure 5.2: Radial profiles of mean axial velocity in a turbulent round jet, $Re = 95,500$. The dashed lines indicate the half-width, $r_{1/2}(x)$, of the profiles. (Adapted from the data of Hussein et al. (1994).)

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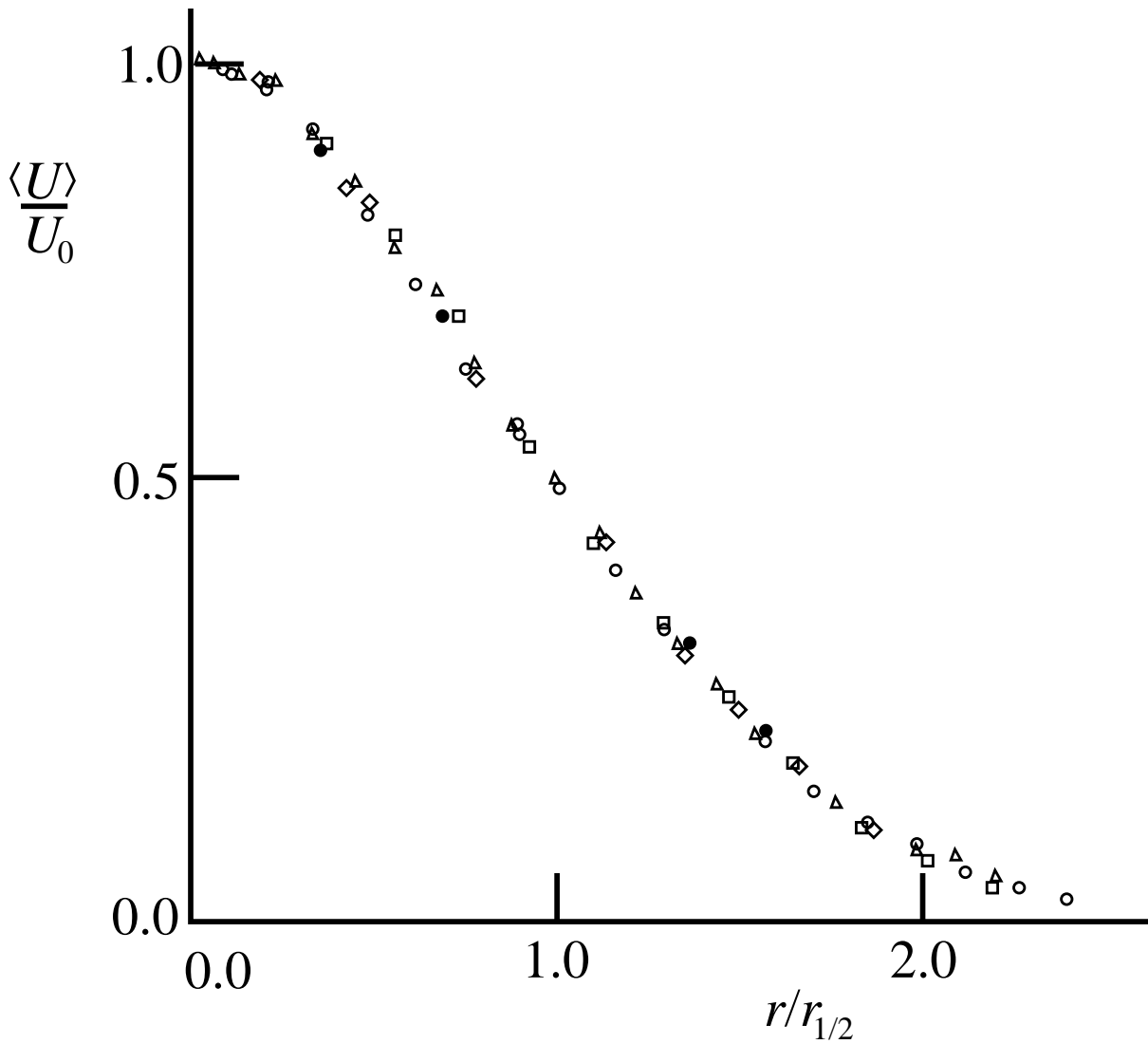


Figure 5.3: Mean axial velocity against radial distance in a turbulent round jet, $Re \approx 10^5$; measurements of Wygnanski and Fiedler (1969). Symbols: \circ , $x/d = 40$; \triangle , 50; \square , 60; \diamond , 75; \bullet , 97.5.

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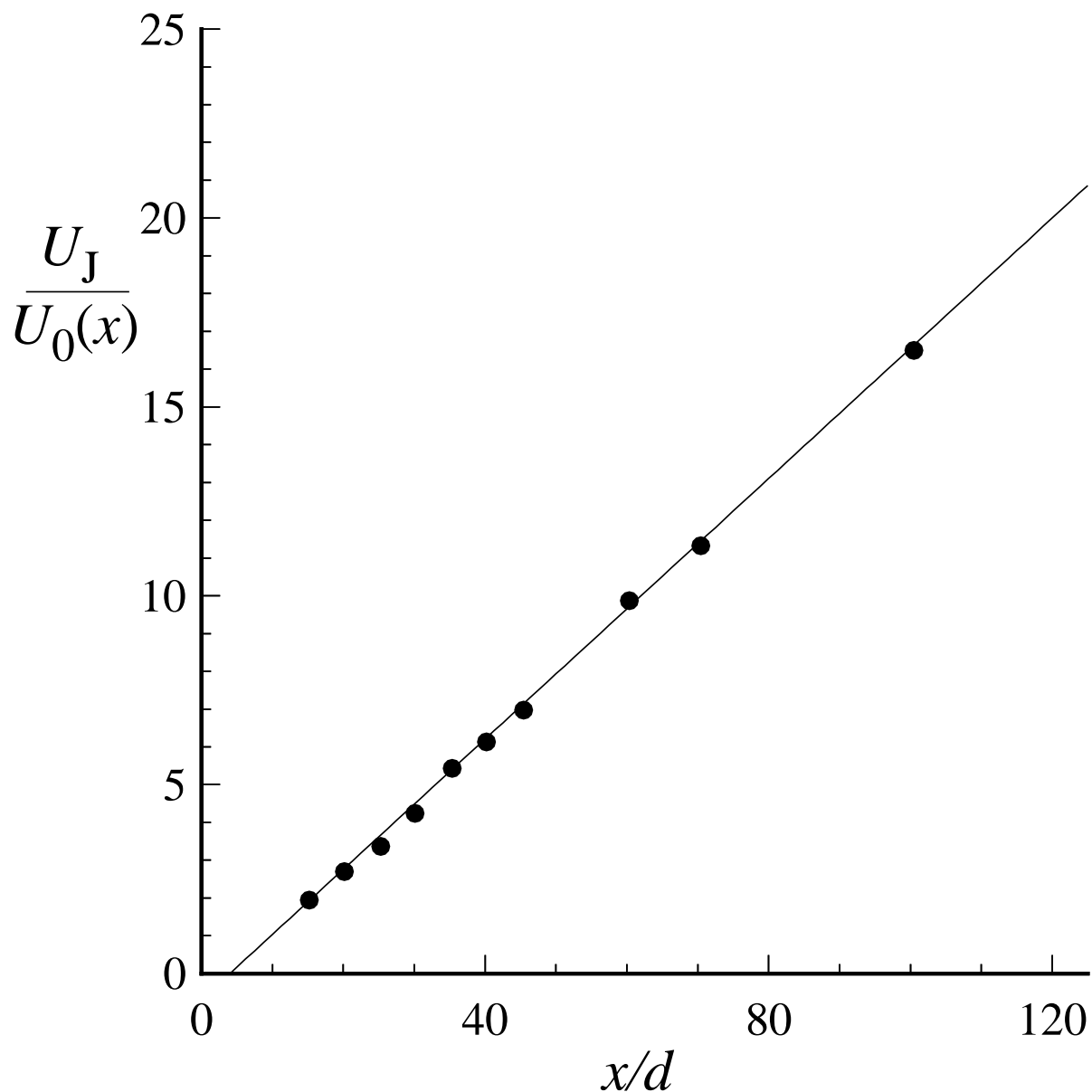


Figure 5.4: Centerline mean velocity variation with axial distance in a turbulent round jet, $Re = 95,500$: symbols, experimental data of Hussein et al. (1994), line—Eq. (5.6) with $x_0/d = 4$, $B = 5.8$.

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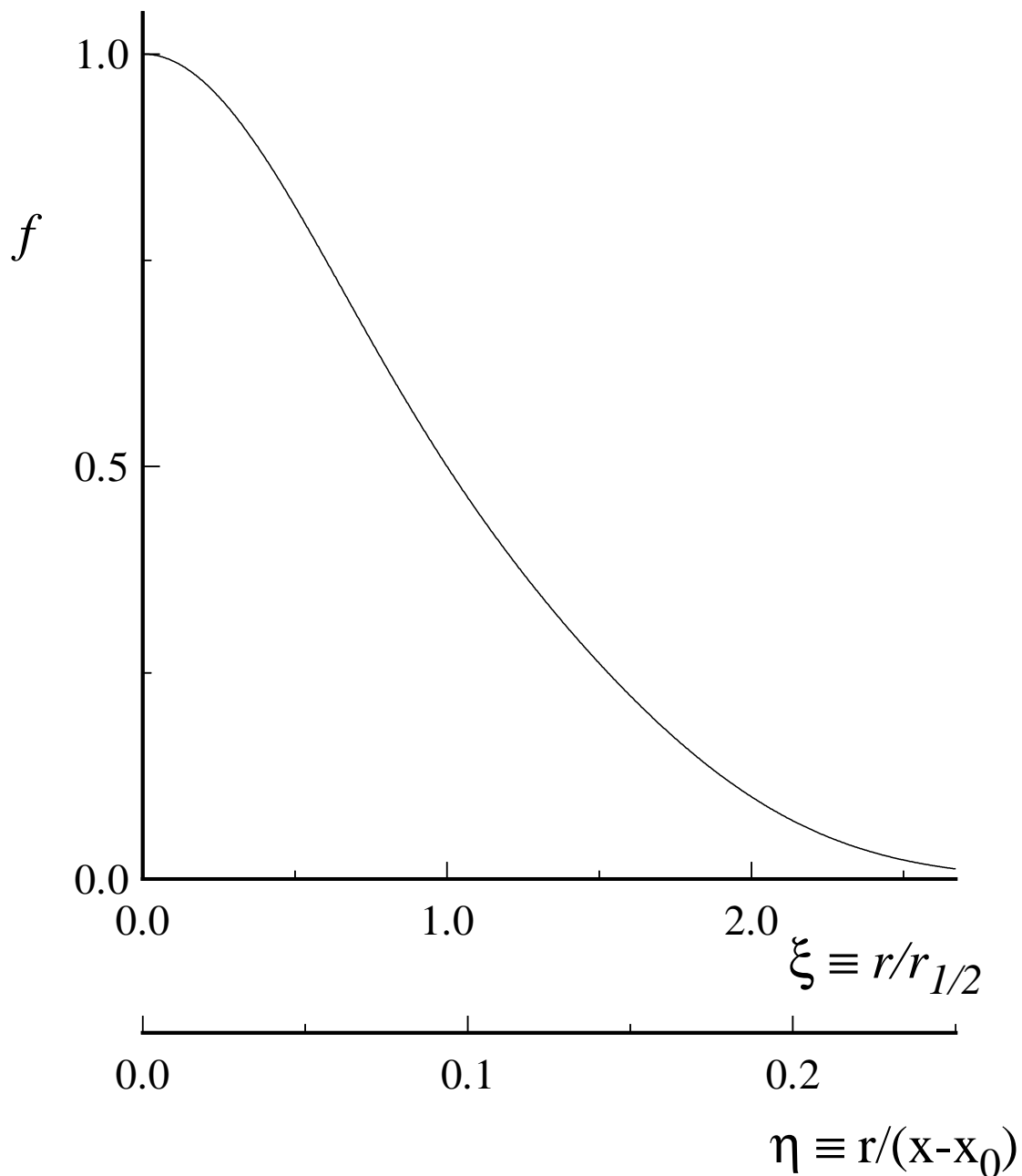


Figure 5.5: Self-similar profile of the mean axial velocity in the self-similar round jet. Curve fit to the LDA data of Hussein et al. (1994).

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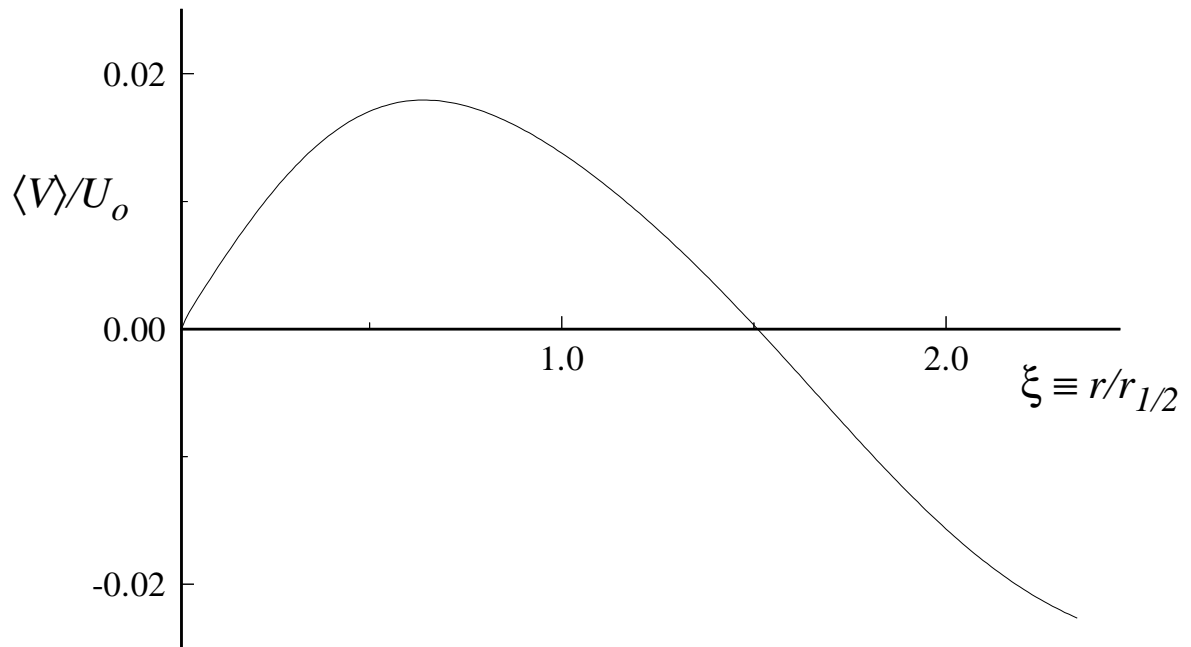


Figure 5.6: Mean lateral velocity in the self-similar round jet. From the LDA data of Hussein et al. (1994).

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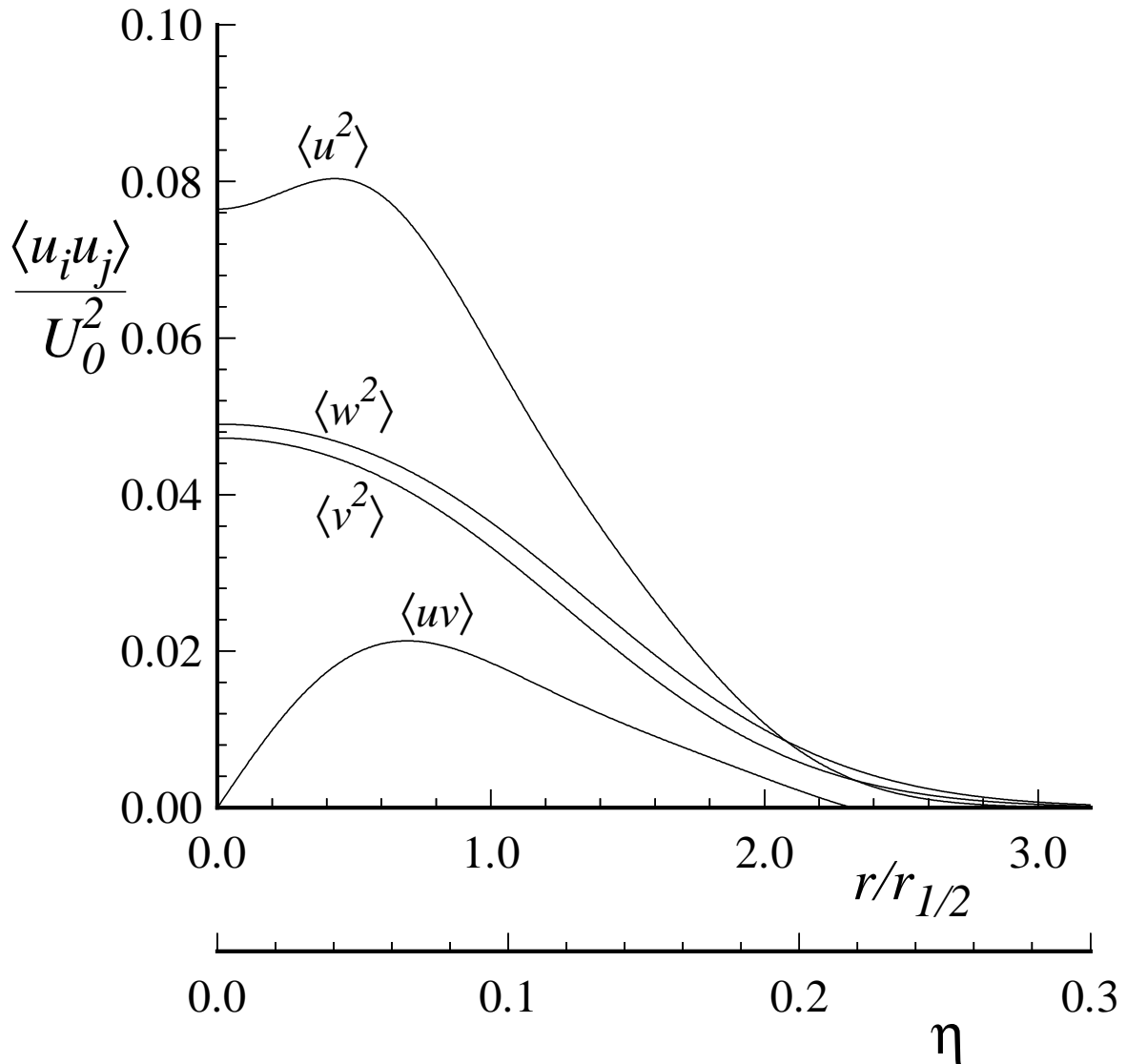


Figure 5.7: Profiles of Reynolds stresses in the self-similar round jet. Curve fit to the LDA data of Hussein et al. (1994).

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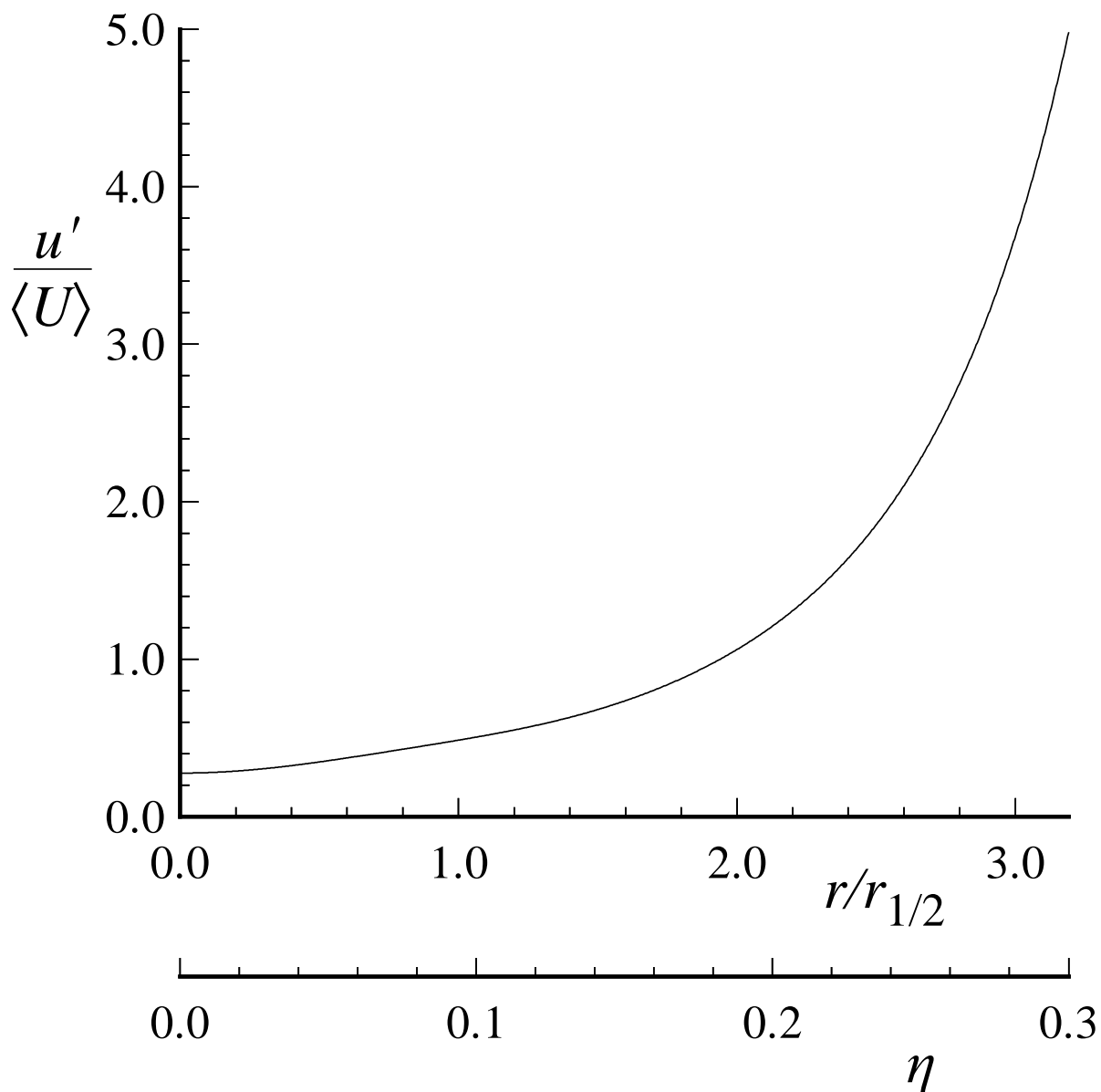


Figure 5.8: Profile of the local turbulence intensity— $\langle u^2 \rangle^{1/2} / \langle U \rangle$ —in the self-similar round jet. From the curve fit to the experimental data of Hussein et al. (1994).

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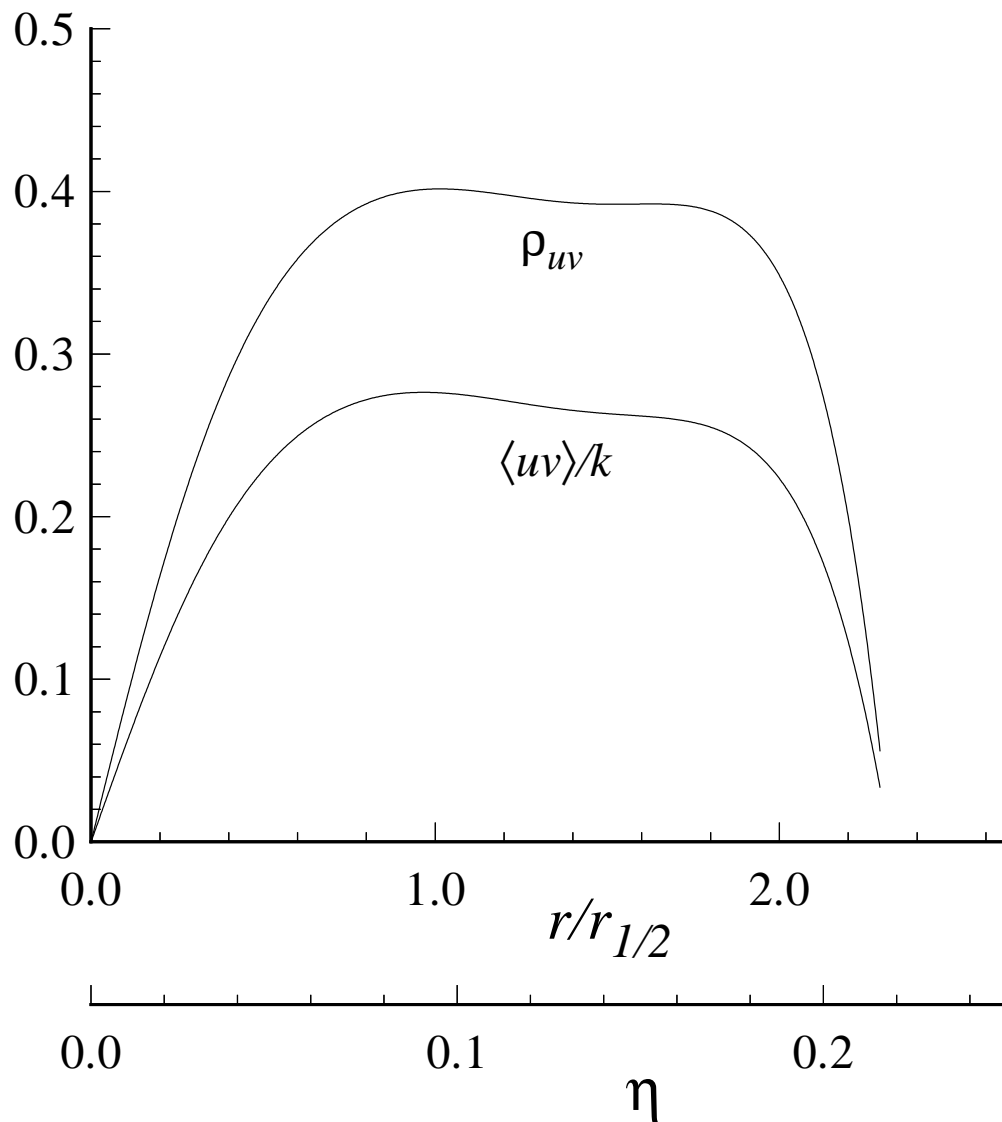


Figure 5.9: Profiles of $\langle uv \rangle / k$ and the $u-v$ correlation coefficient ρ_{uv} in the self-similar round jet. From the curve fit to the experimental data of Hussein et al. (1994).

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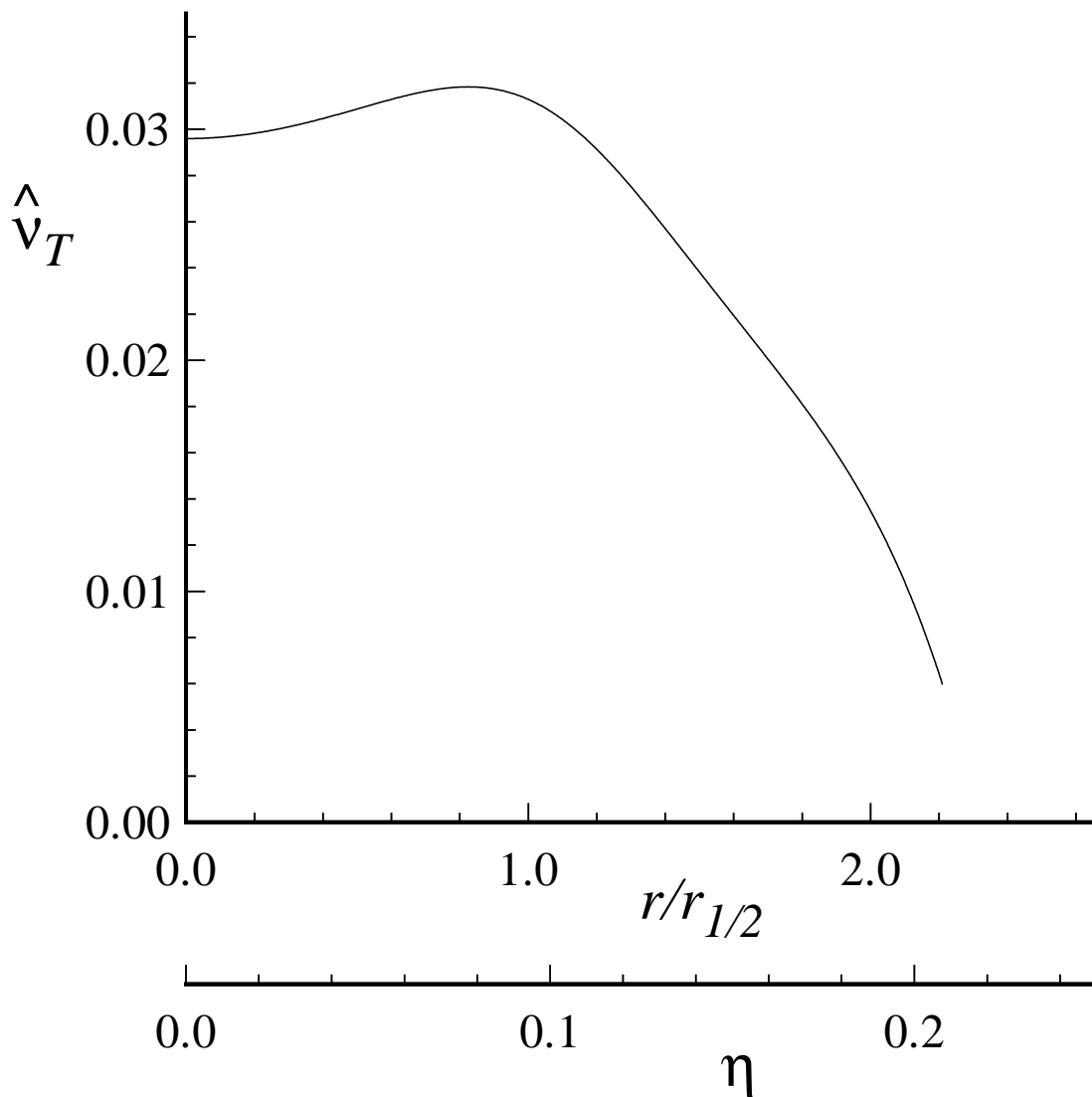


Figure 5.10: Normalized turbulent diffusivity $\hat{\nu}_T$ (Eq. (5.34)) in the self-similar round jet. From the curve fit to the experimental data of Hussein et al. (1994).

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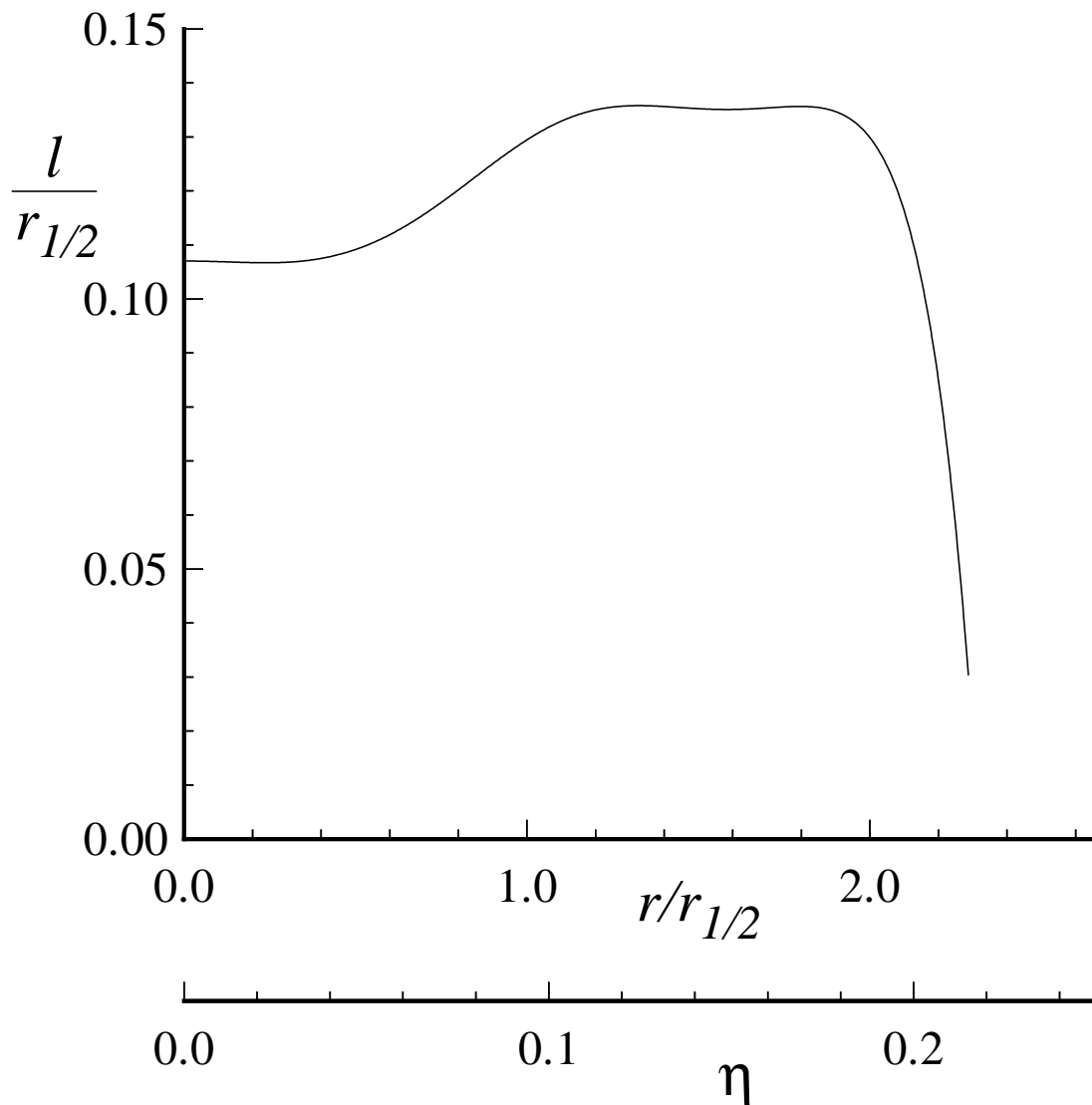


Figure 5.11: Profile of the lengthscale defined by (Eq. (5.35)) in the self-similar round jet. From the curve fit to the experimental data of Hussein et al. (1994).

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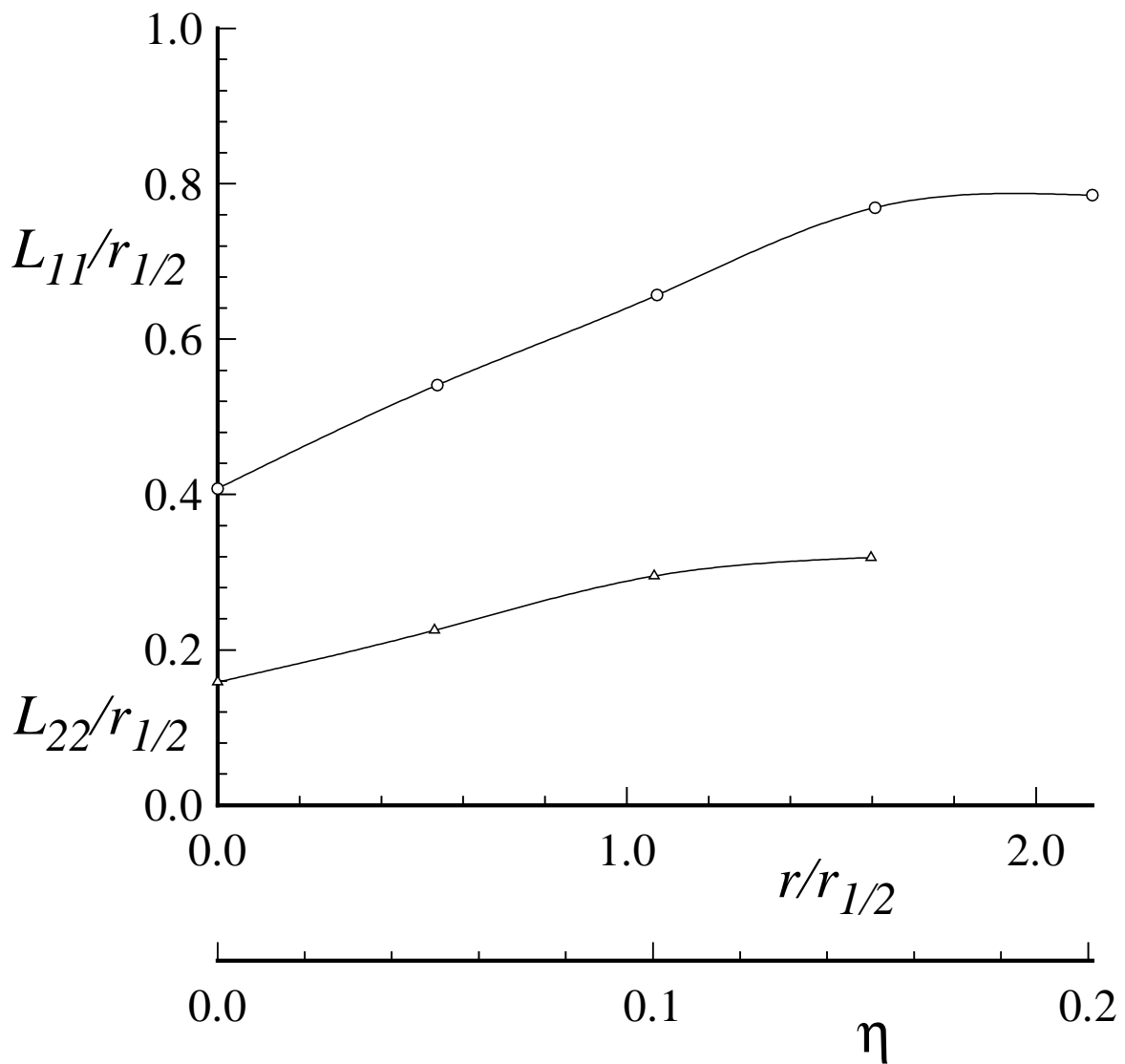


Figure 5.12: Self-similar profiles of the integral lengthscales in the turbulent round jet. From Wygnanski and Fiedler (1969).

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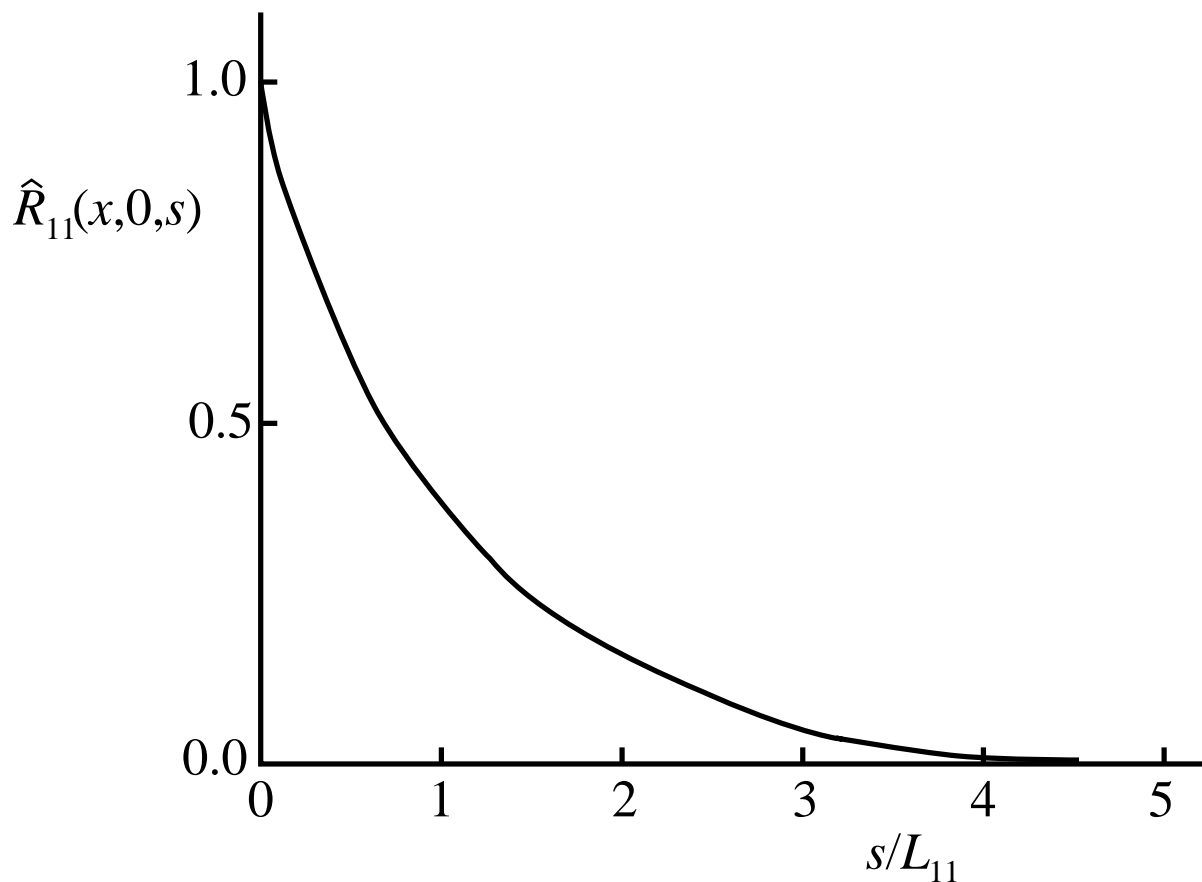


Figure 5.13: Longitudinal autocorrelation of the axial velocity in the self-similar round jet. From Wygnanski and Fiedler (1969).

CHAPTER 5: FREE SHEAR FLOWS

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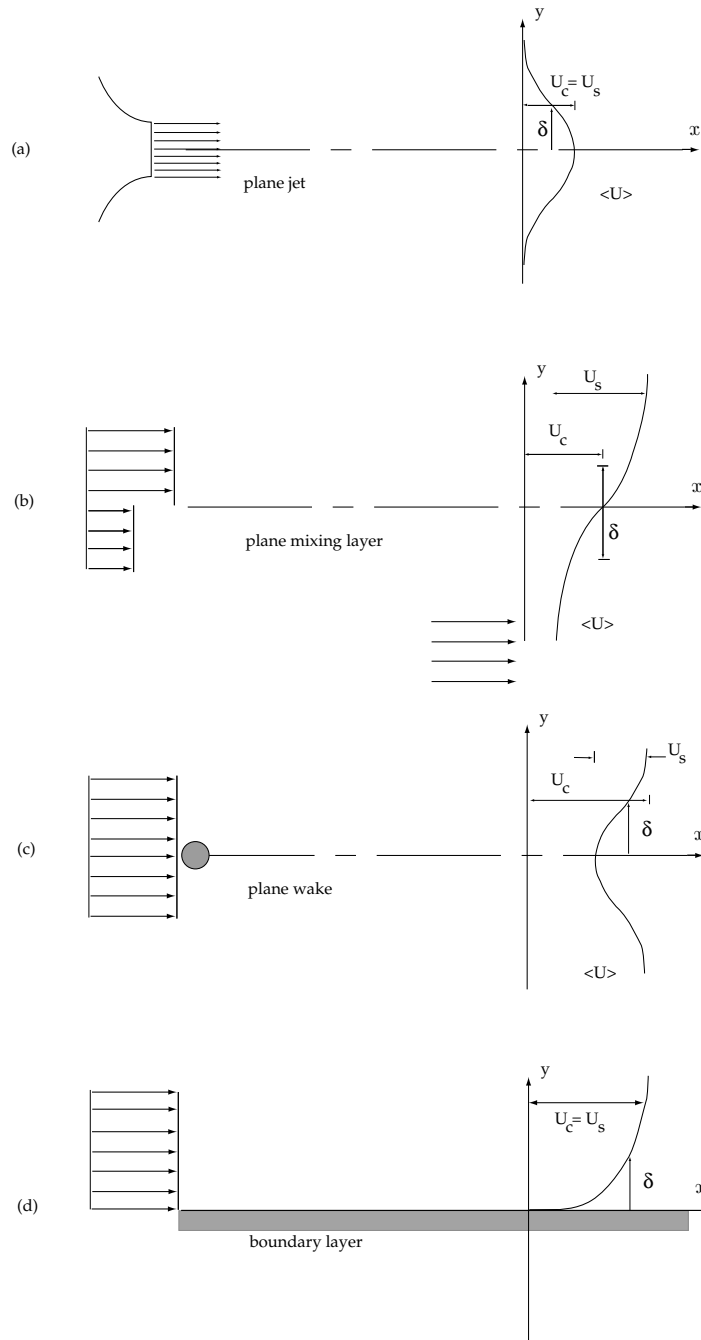


Figure 5.14: Sketch of plane two-dimensional shear flows showing the characteristic flow width $\delta(x)$, the characteristic convective velocity U_c , and the characteristic velocity difference U_s .

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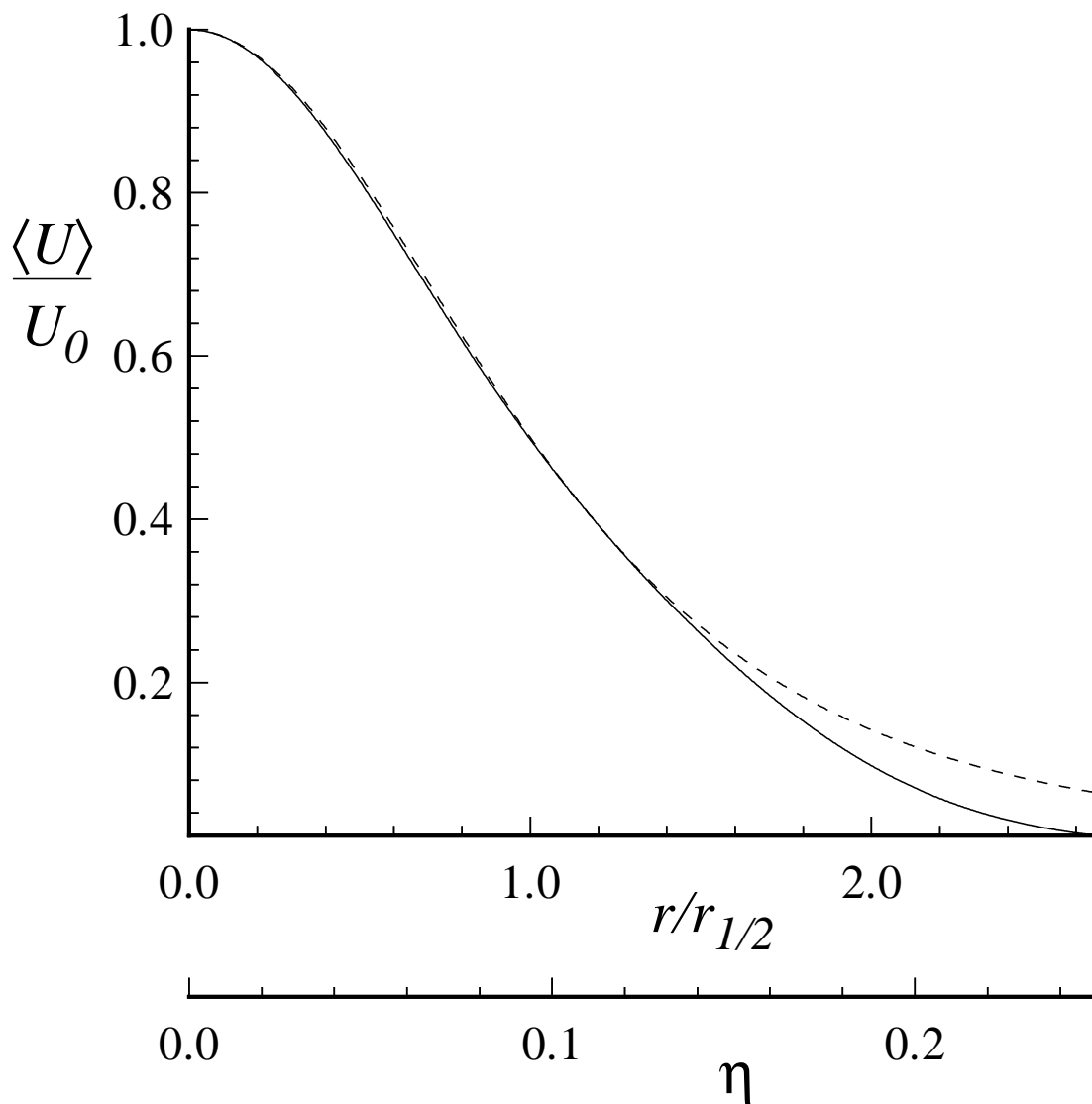


Figure 5.15: Mean velocity profile in the self-similar round jet: solid line, curve fit to the experimental data of Hussein et al. (1994); dashed line, uniform turbulent viscosity solution (Eq. 5.82).

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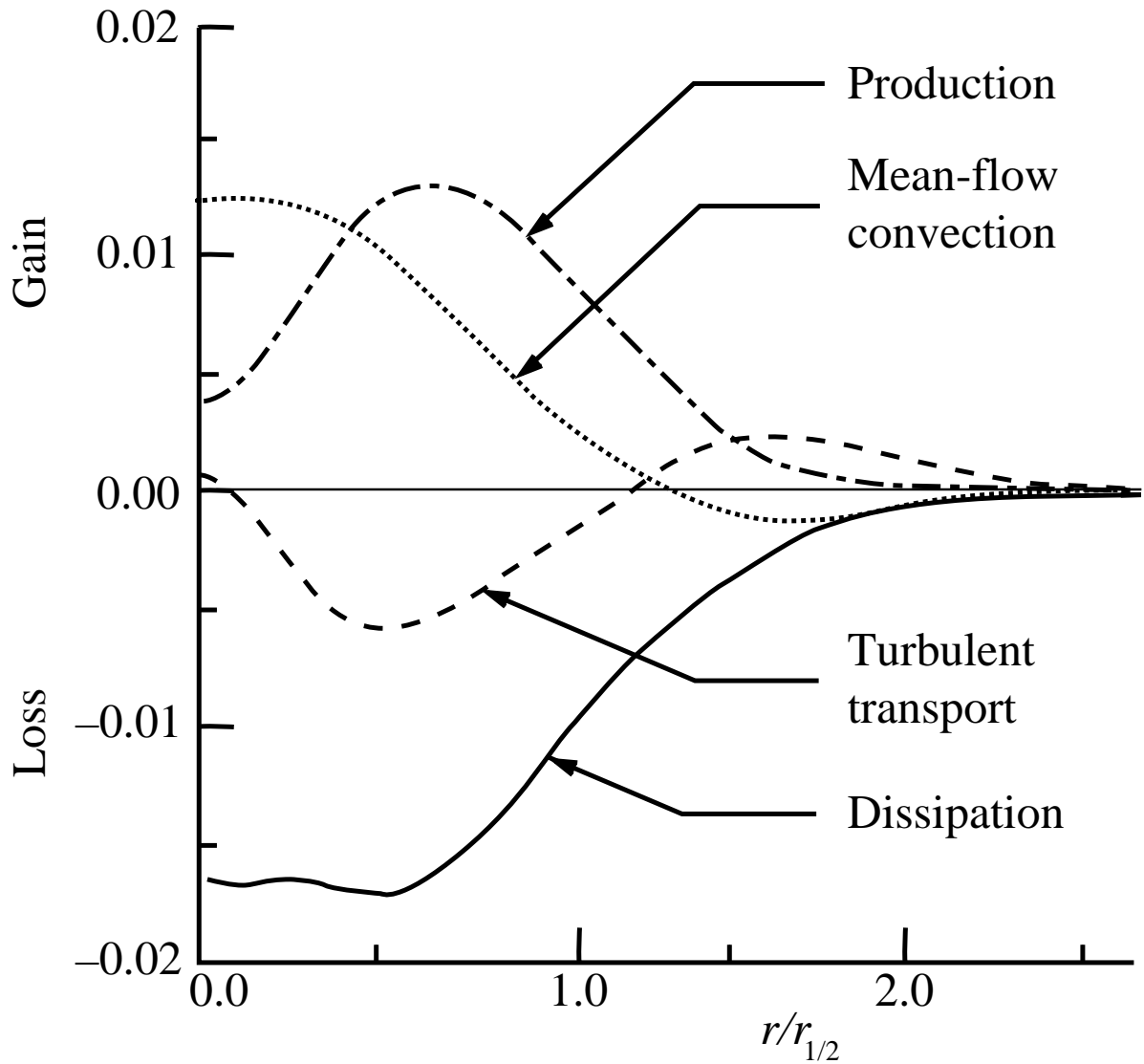


Figure 5.16: Turbulent kinetic energy budget in the self-similar round jet. Quantities are normalized by U_0 and $r_{1/2}$. (From Panchapakesan and Lumley (1993a).)

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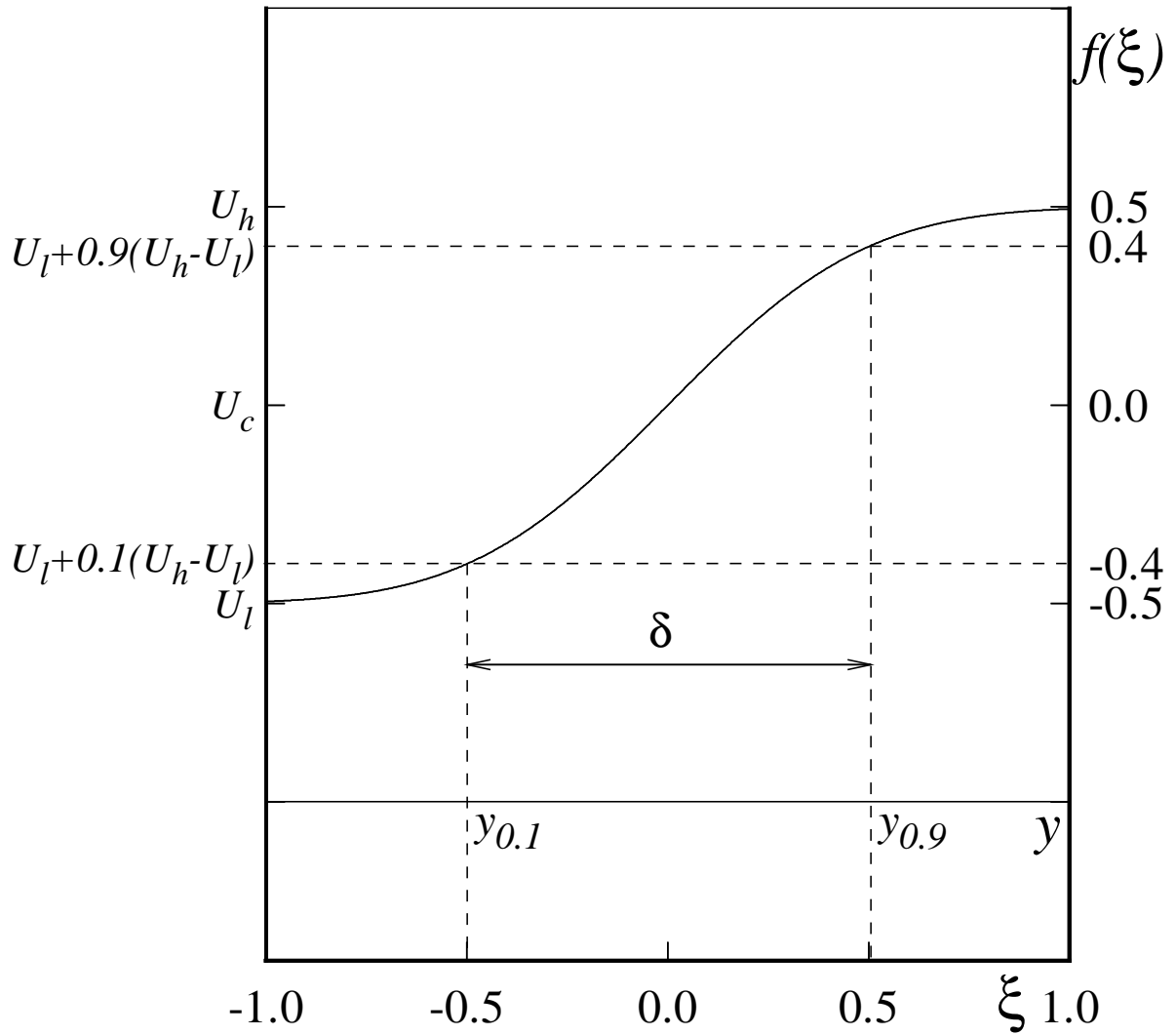


Figure 5.21: Sketch of the mean velocity $\langle U \rangle$ against y , and of the scaled mean velocity profile $f(\xi)$, showing the definitions of $y_{0.1}$, $y_{0.9}$ and δ .

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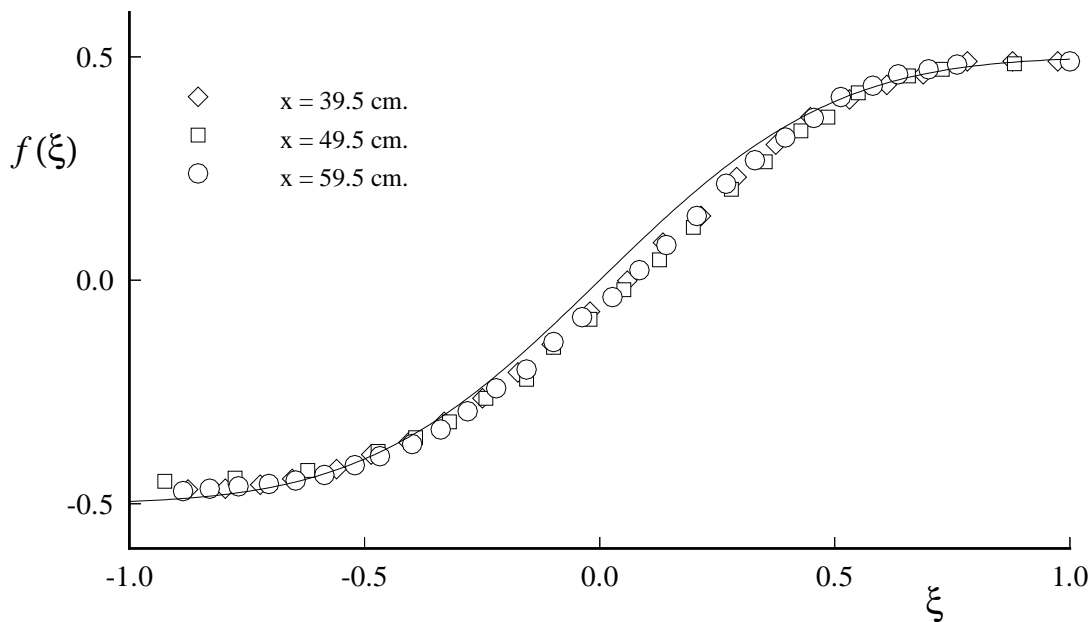


Figure 5.22: Scaled velocity profiles in a plane mixing layer. Symbols, experimental data of Champagne et al. (1976); line, error-function profile (Eq. (5.224)) shown for reference.

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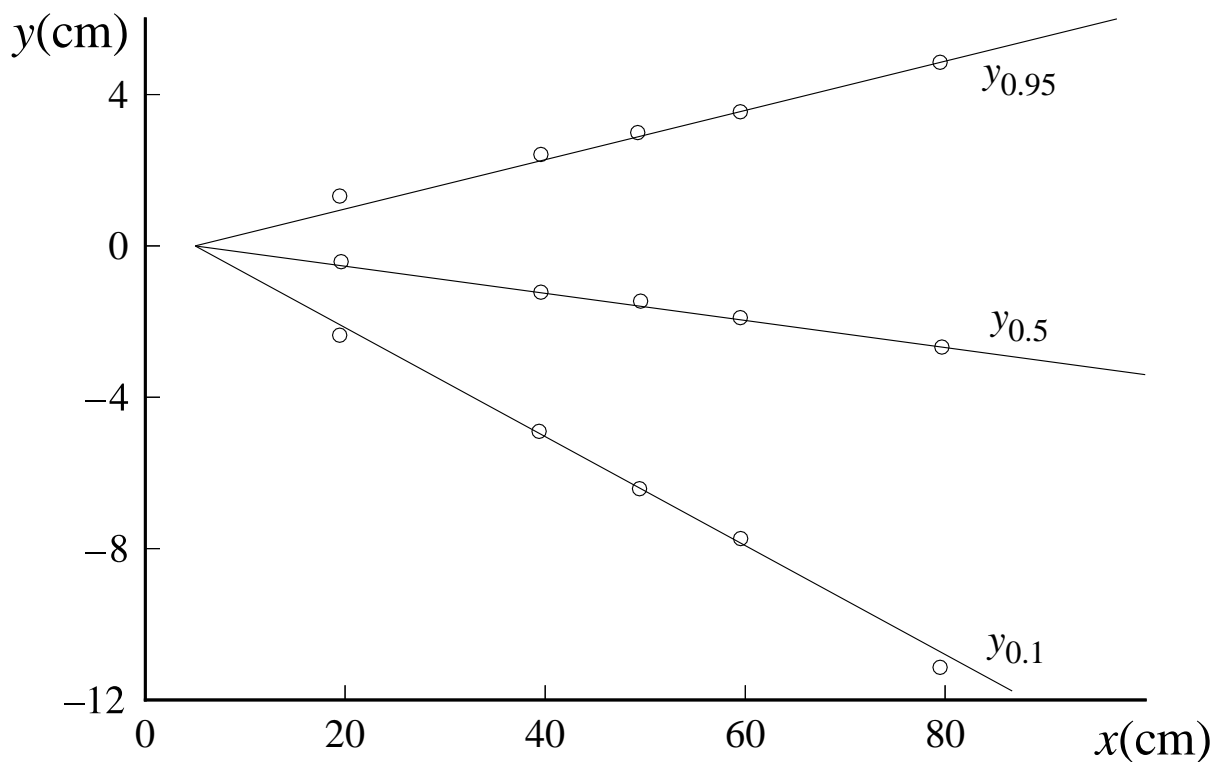


Figure 5.23: Axial variation of $y_{0.1}$, $y_{0.5}$ and $y_{0.95}$ in the plane mixing layer, showing the linear spreading. Experimental data of Champagne et al. (1976).

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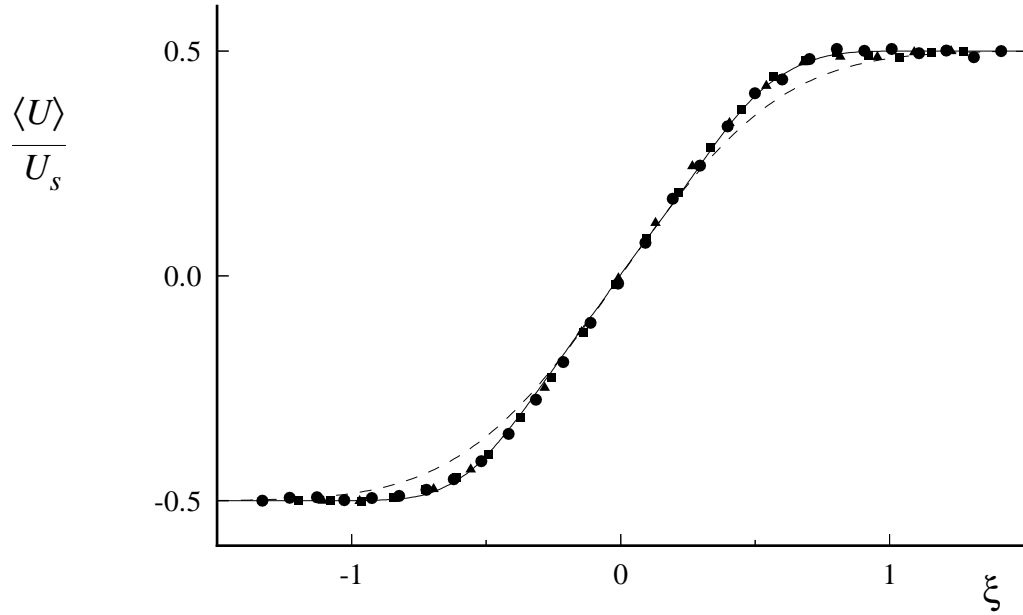


Figure 5.24: Scaled mean velocity profile in self-similar plane mixing layers. Symbols, experiment of Bell and Mehta (1990) ($U_\ell/U_h = 0.6$); solid line, DNS data for the temporal mixing layer (Rogers and Moser 1994); dashed line error-function profile with width chosen to match data in the center of the layer.

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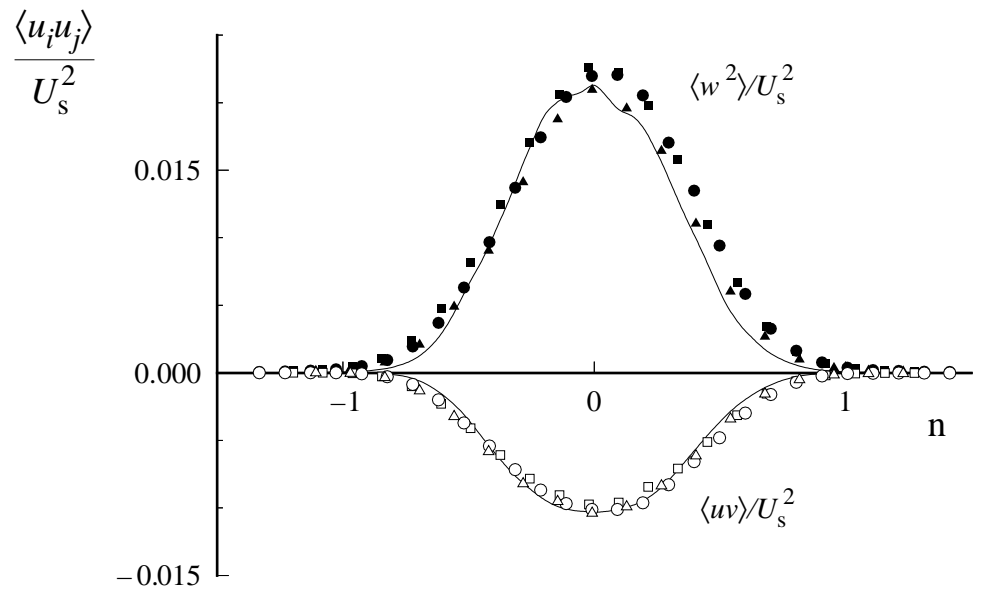
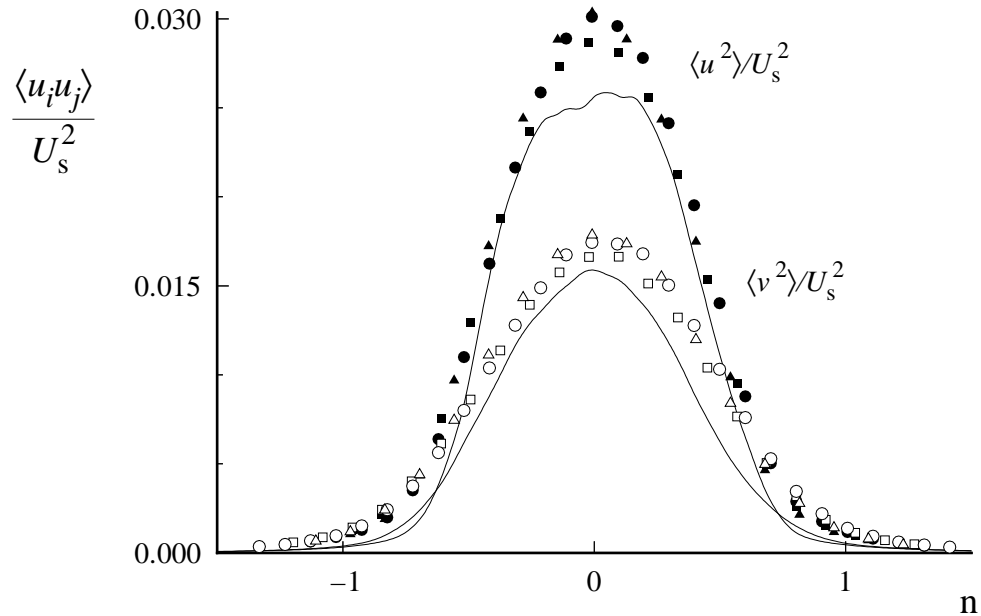


Figure 5.25: Scaled Reynolds stress profiles in self-similar plane mixing layers. Symbols, experiment of Bell and Mehta (1990) ($U_\ell/U_h = 0.6$); solid line, DNS data for the temporal mixing layer (Rogers and Moser 1994).

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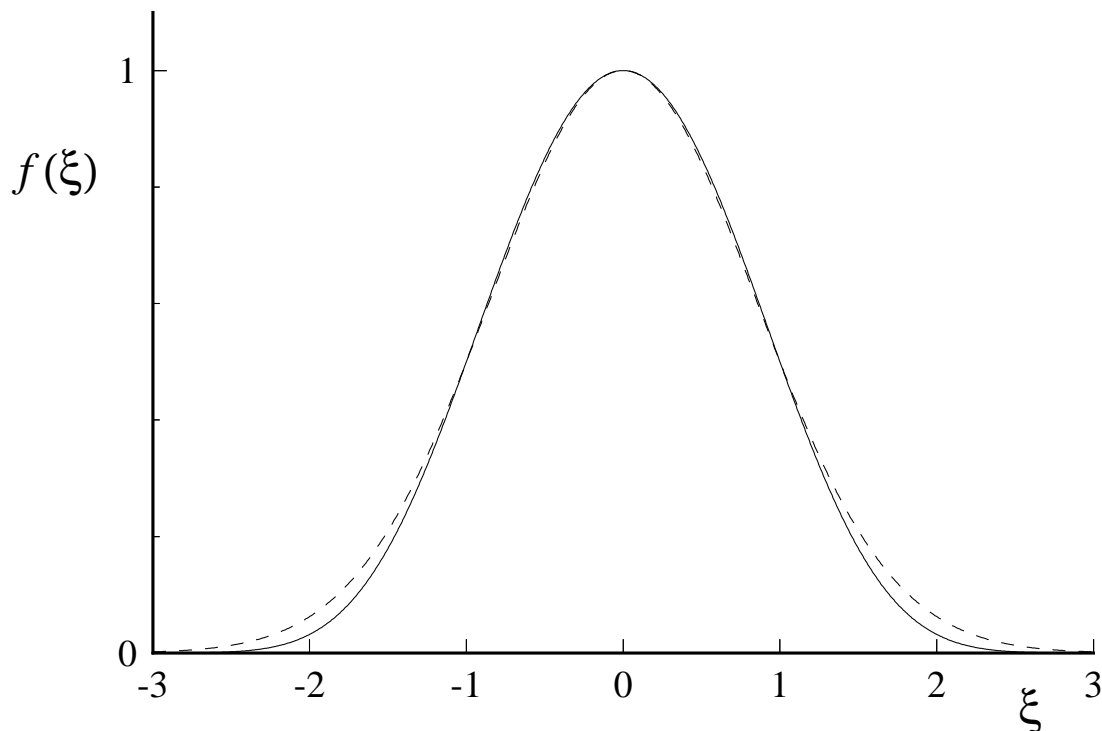


Figure 5.26: Normalized velocity defect profile in the self-similar plane wake. Solid line, from experimental data of Wygnanski et al. (1986); dashed line, constant-turbulent-viscosity solution, Eq. (5.240).

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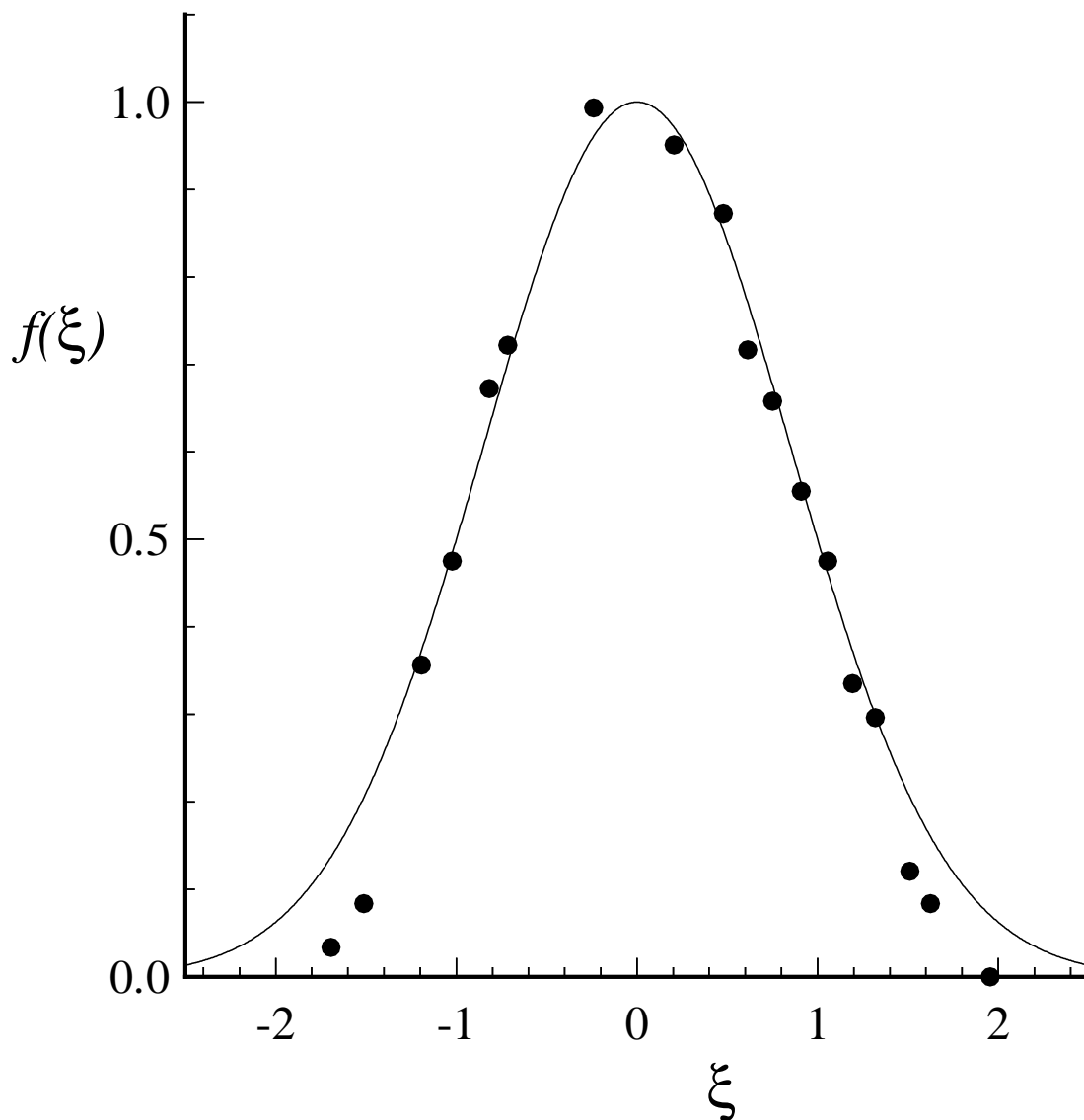


Figure 5.27: Mean velocity deficit profiles in a self-similar axisymmetric wake. Symbols, experimental data of Uberoi and Freymuth (1970); line, constant-turbulent-viscosity solution $f(\xi) = \exp(-\xi^2 \ln 2)$

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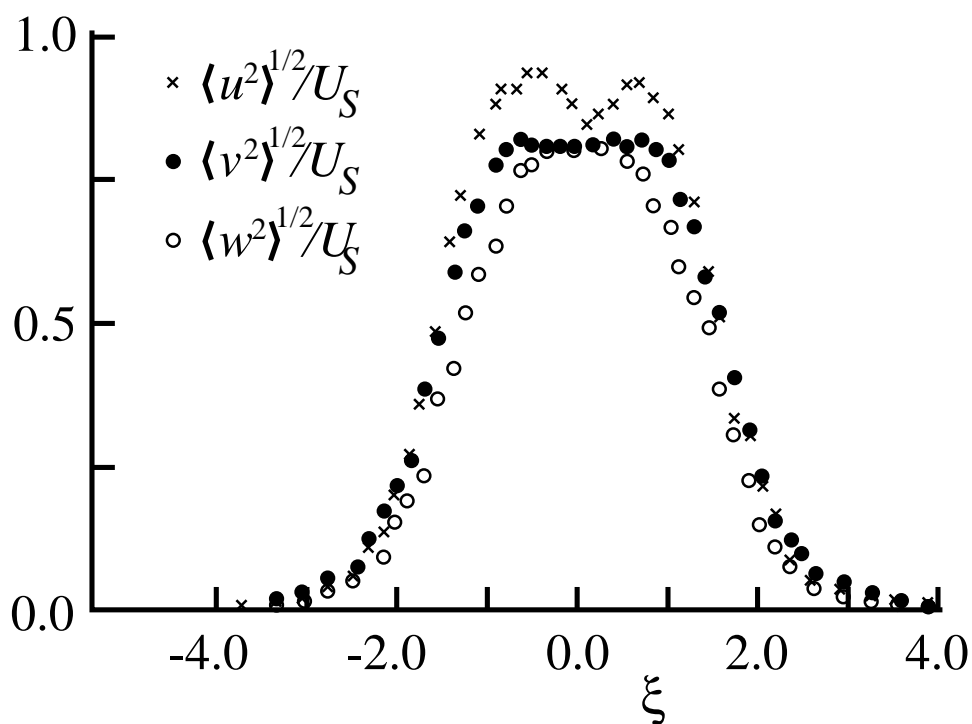


Figure 5.28: R.m.s. velocity profiles in a self-similar axisymmetric wake. Experimental data of Uberoi and Freymuth (1970).

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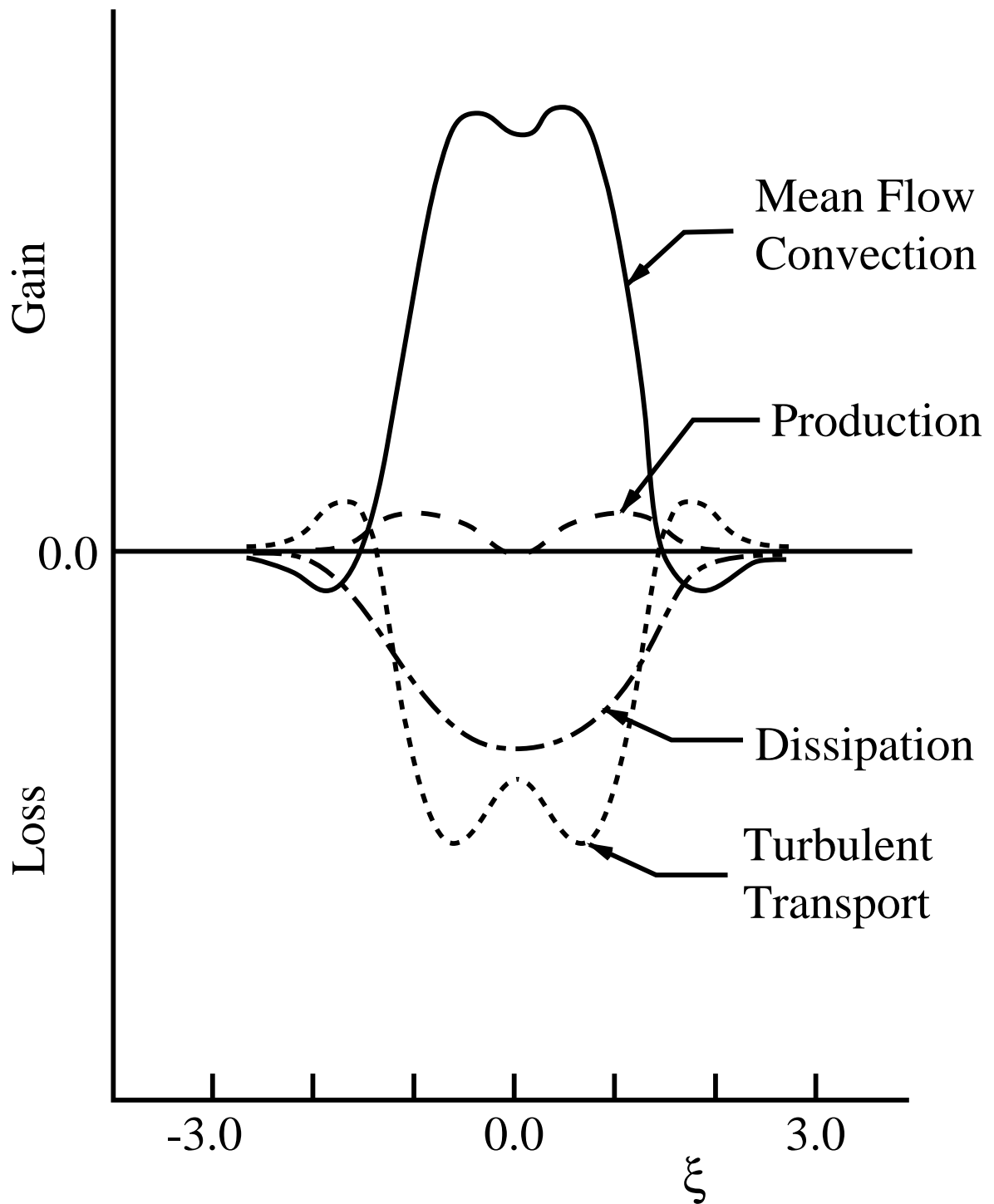


Figure 5.29: Turbulent kinetic energy budget in a self-similar axisymmetric wake. Experimental data of Uberoi and Freymuth (1970).

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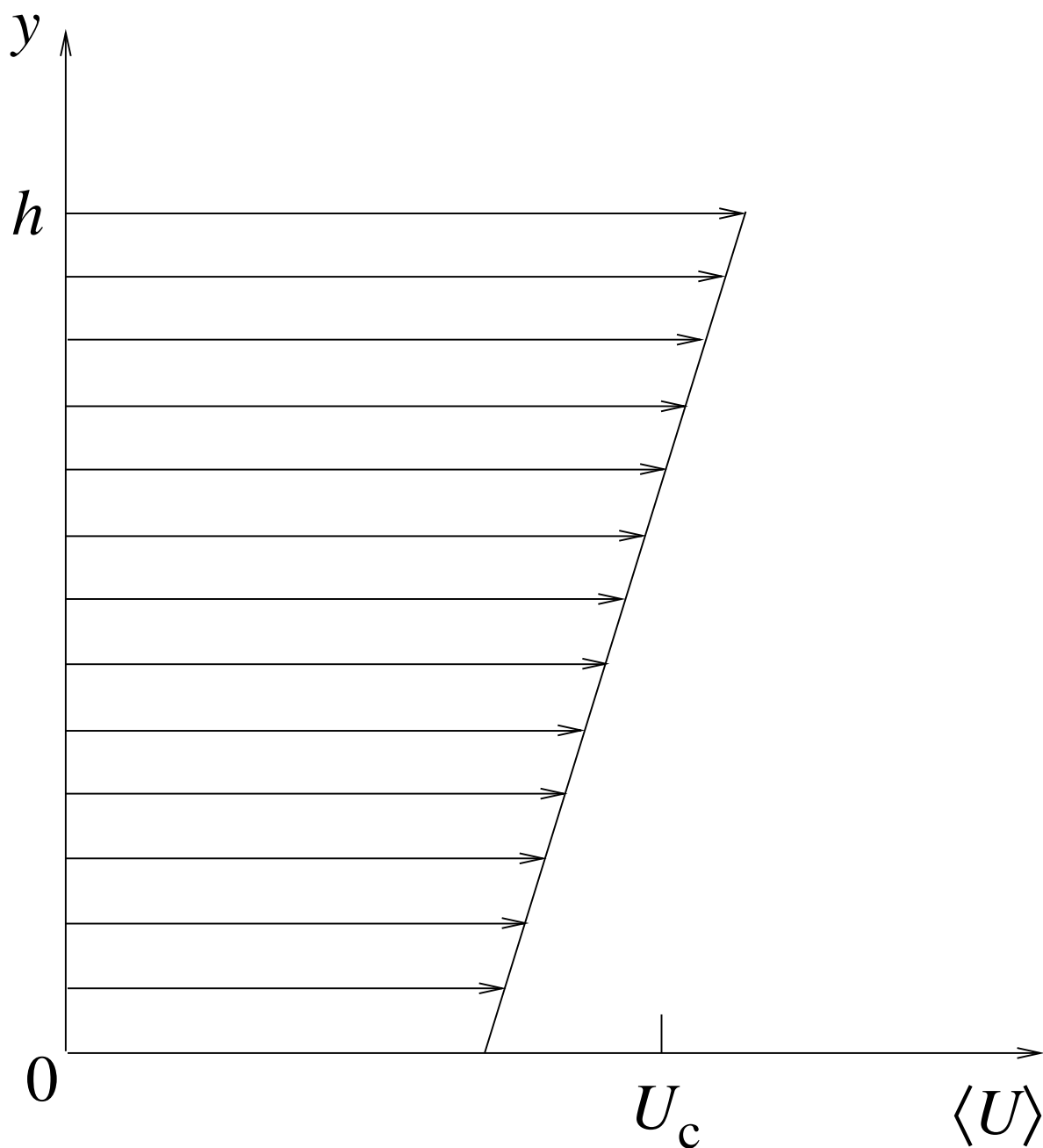


Figure 5.30: Sketch of the mean velocity profile in homogeneous shear flow.

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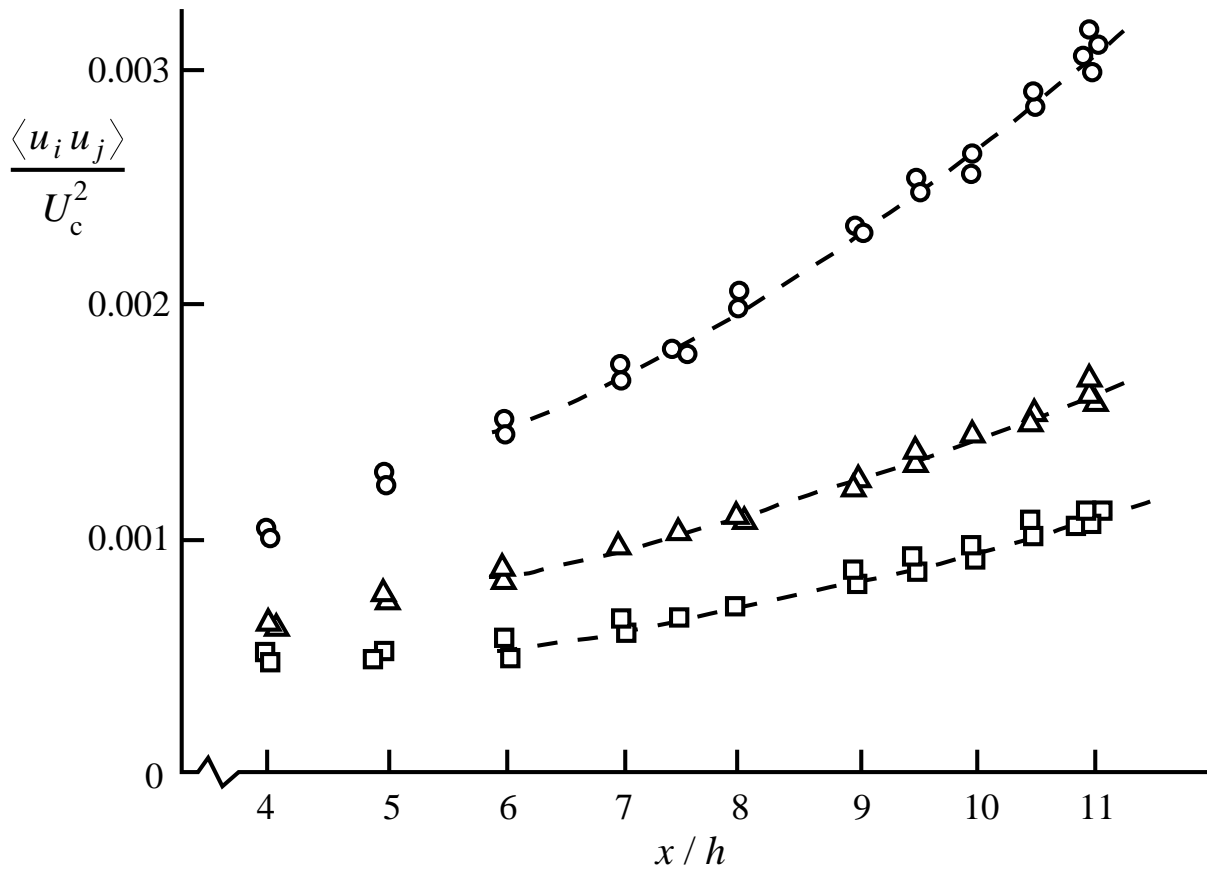


Figure 5.31: Reynolds stresses against axial distance in the homogeneous shear flow experiment of Tavoularis and Corrsin (1981): ○, $\langle u^2 \rangle$; □, $\langle v^2 \rangle$; △, $\langle w^2 \rangle$.

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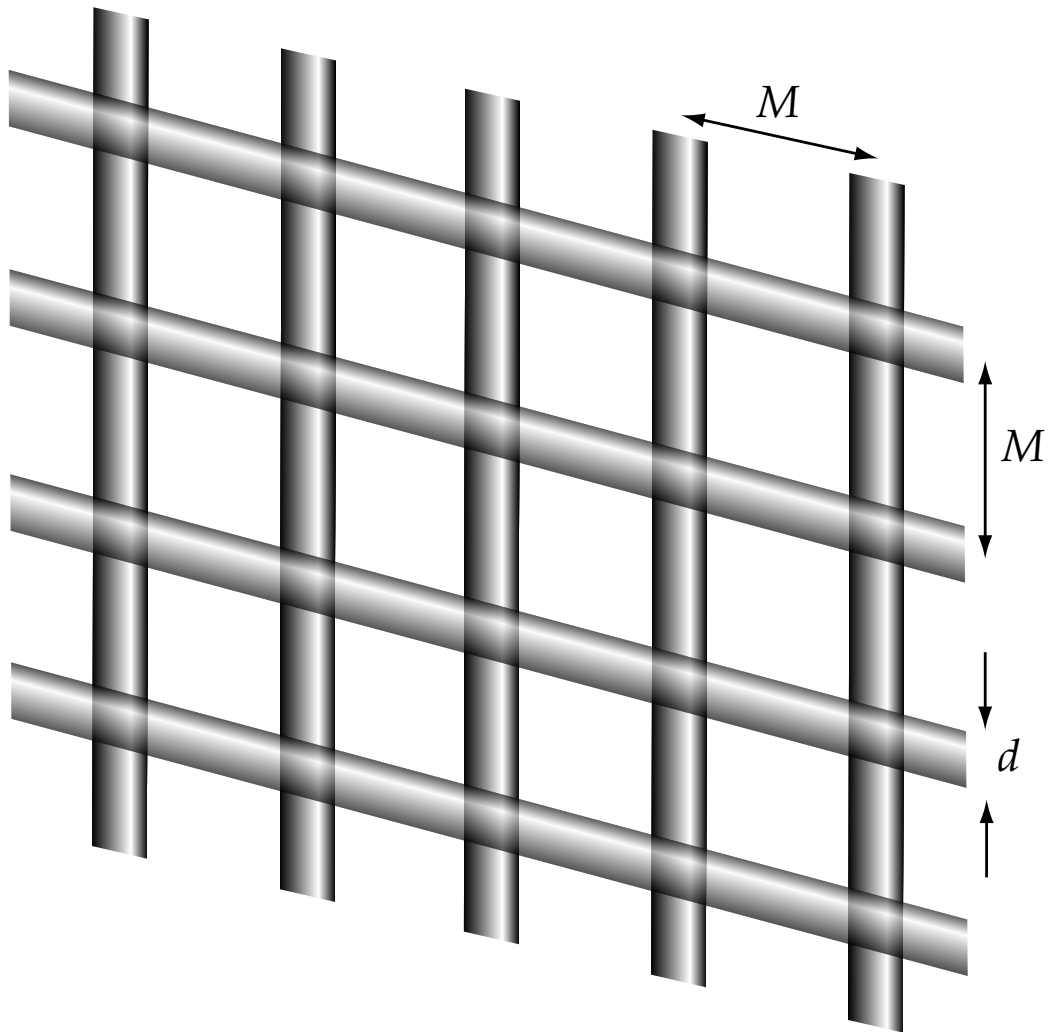


Figure 5.32: Sketch of a turbulence generating grid composed of bars of diameter d , with mesh spacing M .

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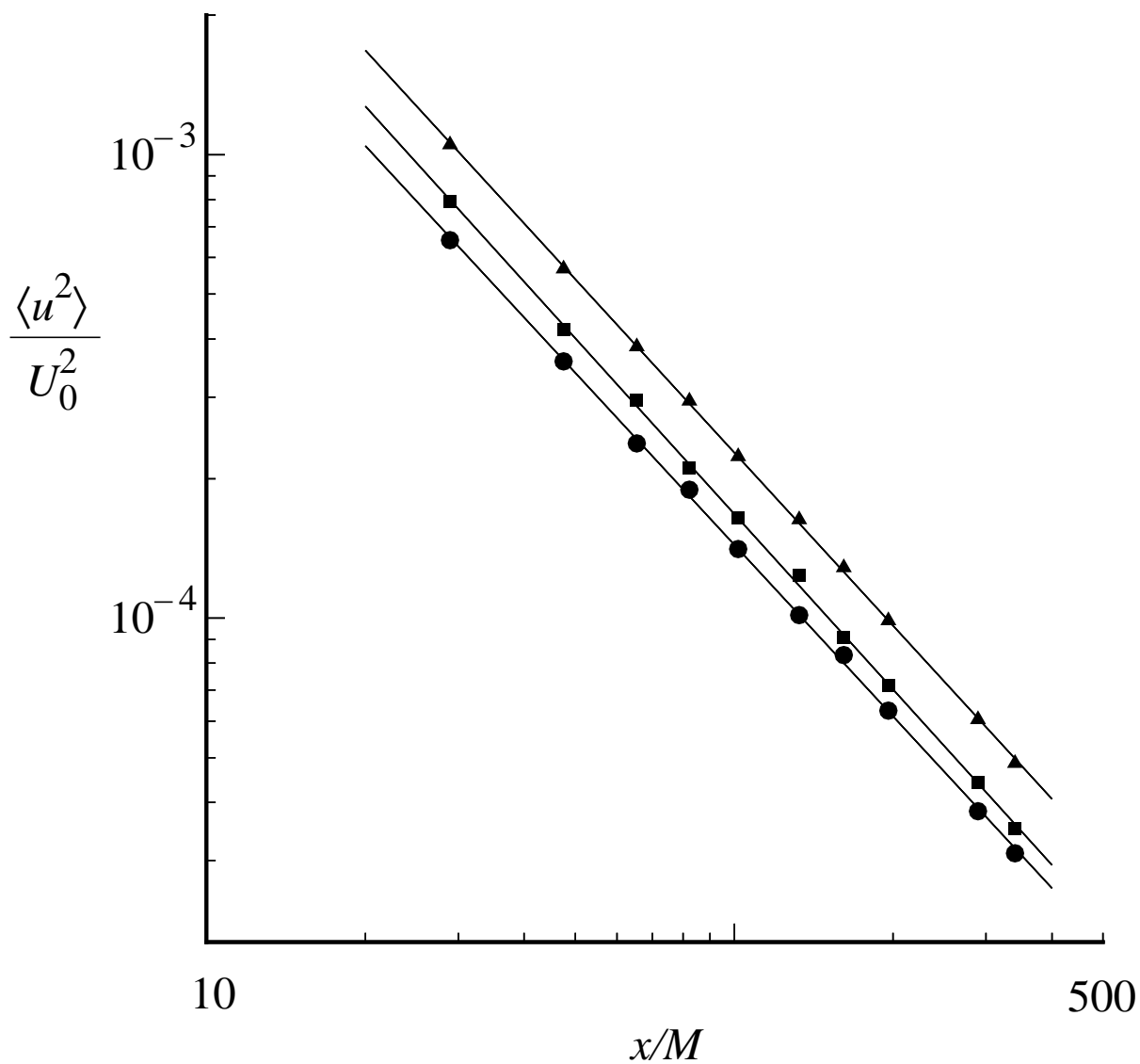


Figure 5.33: Decay of Reynolds stresses in grid turbulence: squares $\langle u^2 \rangle / U_0^2$; circles $\langle v^2 \rangle / U_0^2$; triangles k / U_0^2 ; lines, proportional to $(x/M)^{-1.3}$. (From Comte-Bellot and Corrsin (1966).)

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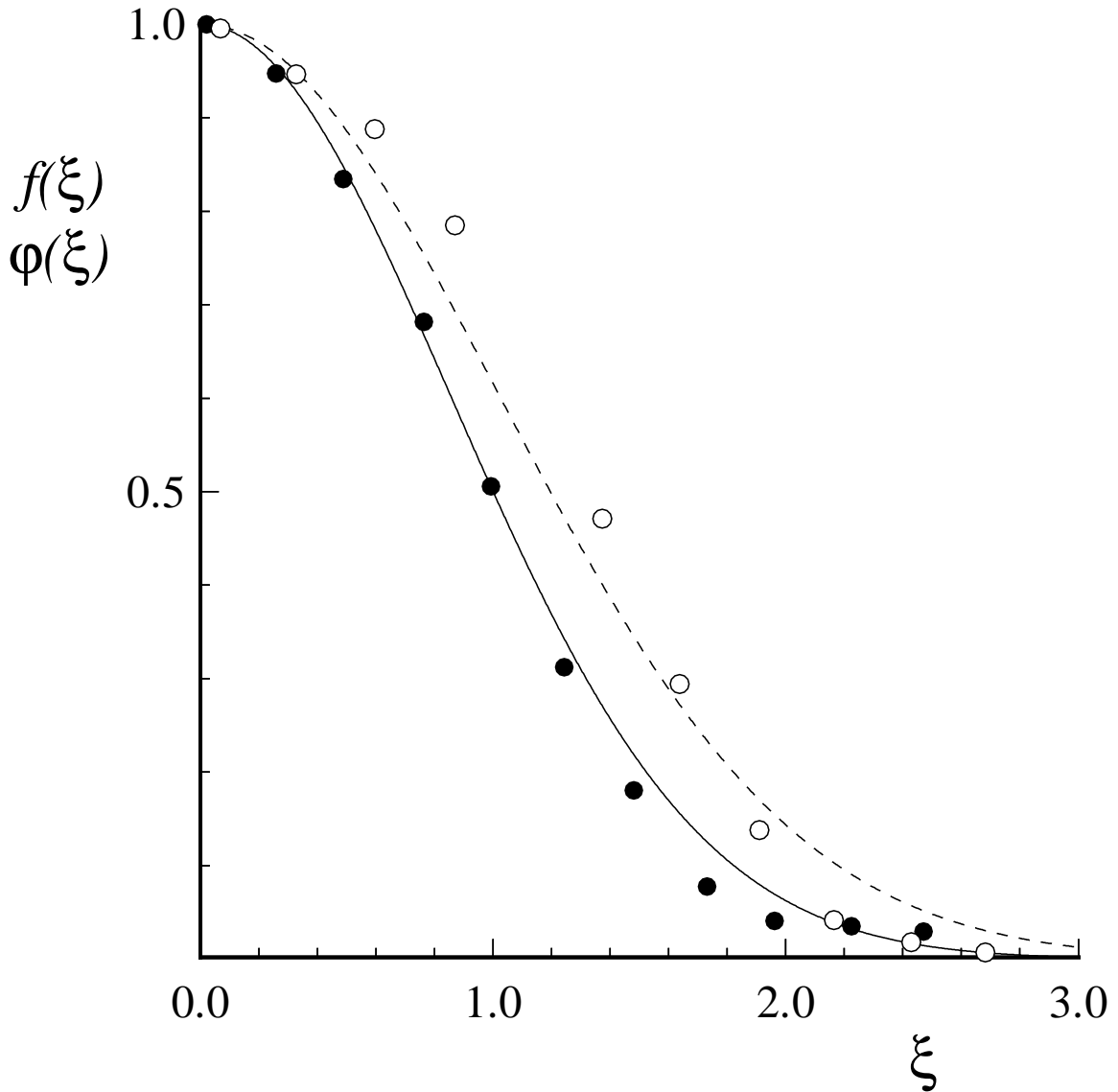


Figure 5.34: Normalized mean velocity deficit $f(\xi)$ and scalar, $\varphi(\xi) = \langle \phi \rangle / \langle \phi \rangle_{y=0}$ in the self-similar plane wake. Symbols (solid f , open φ) experimental data of Fabris (1979); solid line, $f(\xi) = \exp(-\xi^2 \ln 2)$; dashed line, $\varphi(\xi) = \exp(-\xi^2 \sigma_T \ln 2)$ with $\sigma_T = 0.7$.

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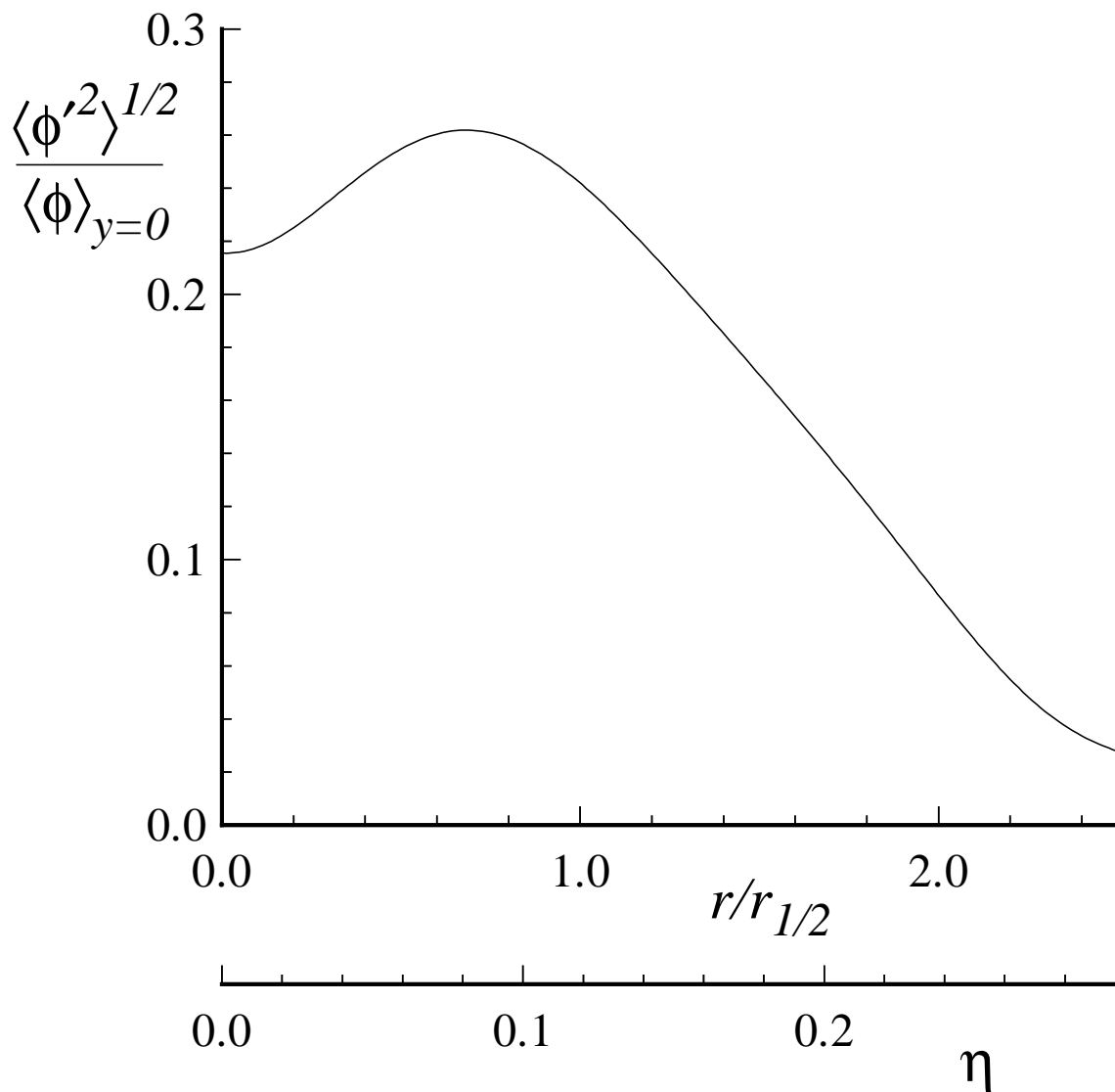


Figure 5.35: Normalized r.m.s. scalar fluctuations in a round jet. From the experimental data of Panchapakesan and Lumley (1993b).

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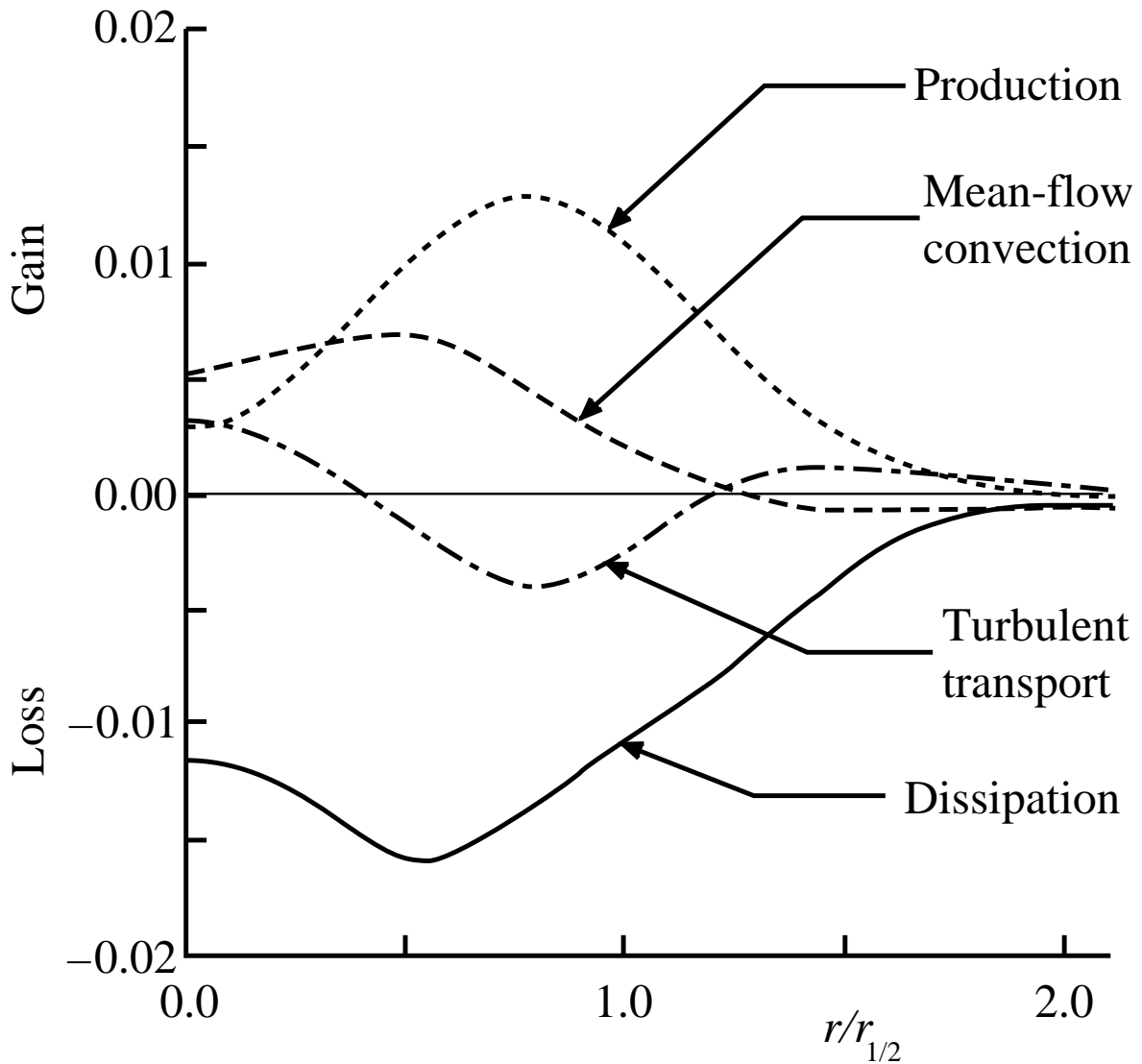


Figure 5.36: Scalar variance budget in a round jet: terms in Eq. (5.281) normalized by $\langle \phi \rangle_{y=0}$, U_s and $r_{1/2}$. (From the experiment data of Panchapakesan and Lumley (1993b).)

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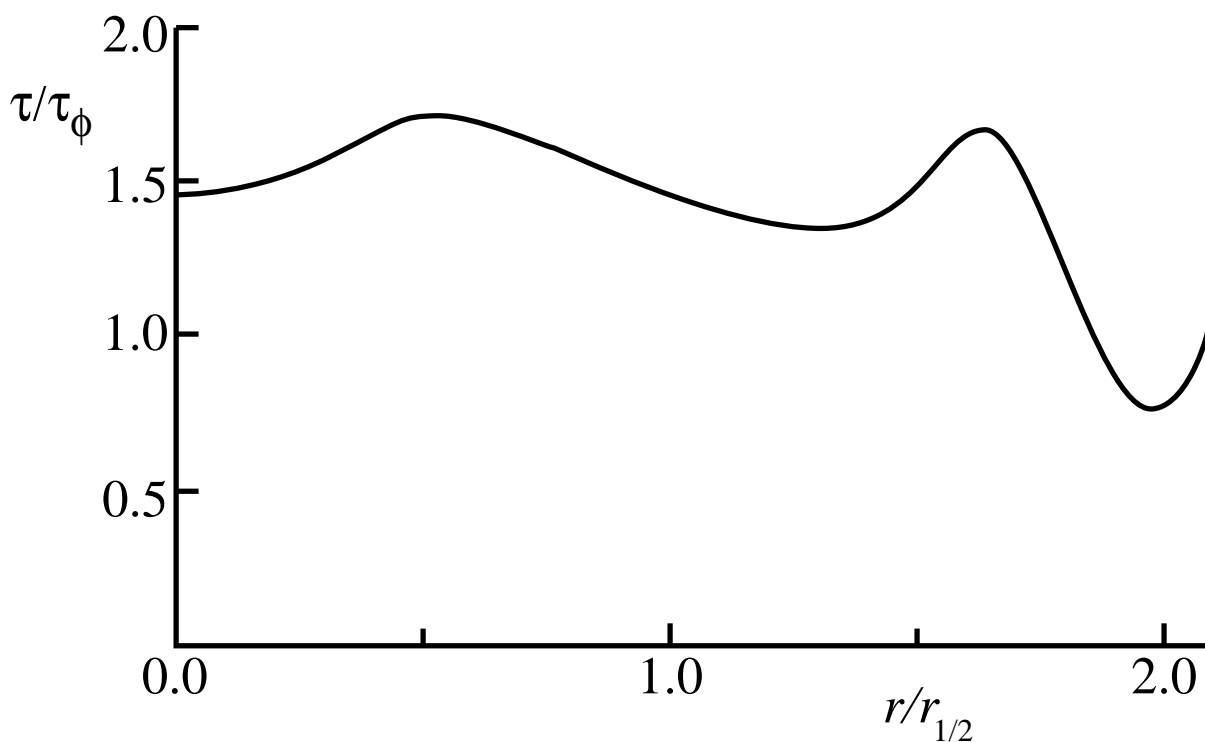


Figure 5.37: Scalar-to-velocity timescale ratio in a round jet. (From the experimental data of Panchapakesan and Lumley (1993b).)

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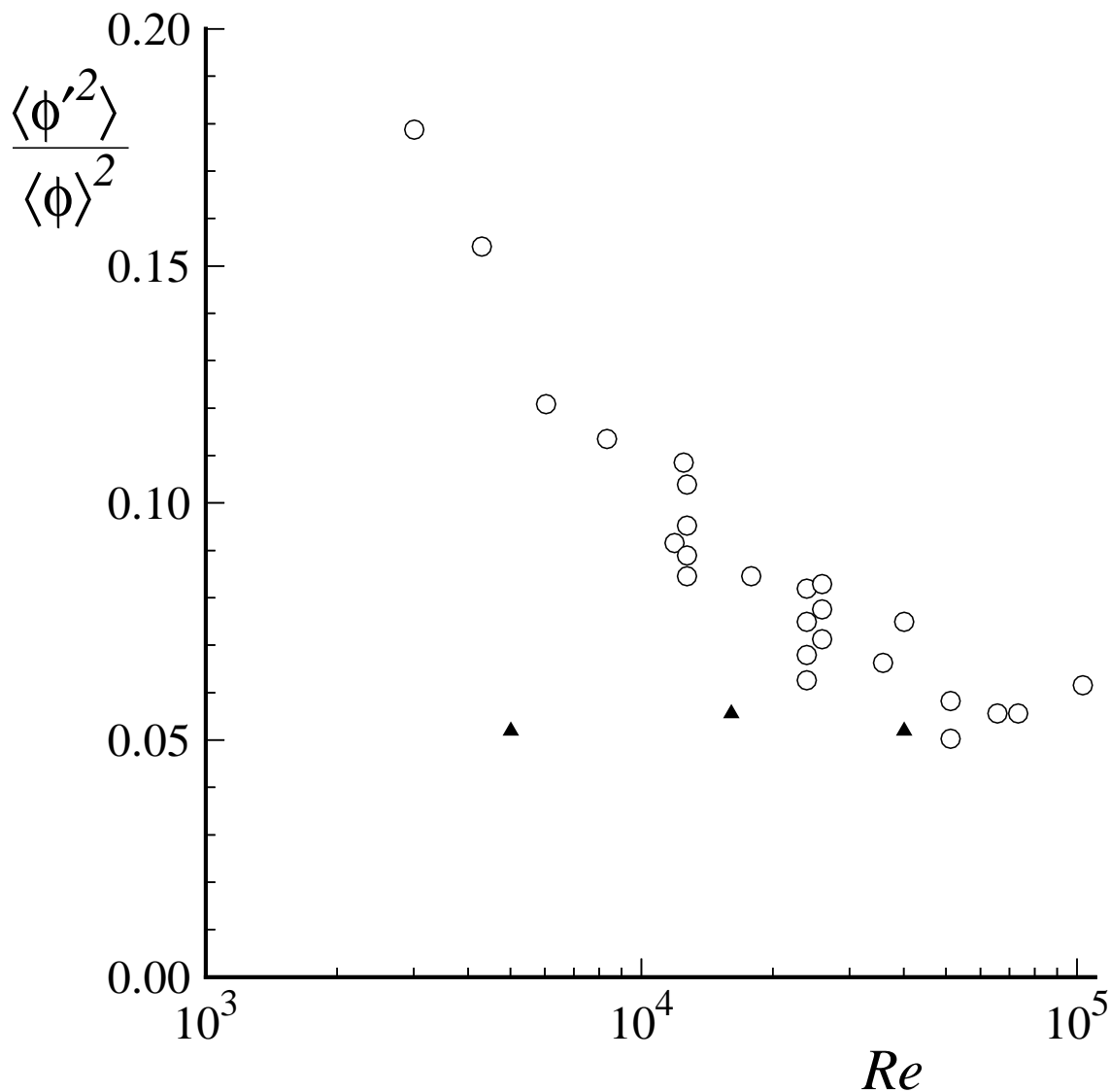


Figure 5.38: Normalized scalar variance on the axis of self-similar round jets at different Reynolds numbers. Triangles, air jets (experiments of Dowling and Dimotakis (1990)); circles, water jets (experiments of Miller (1991)). (From Miller (1991).)

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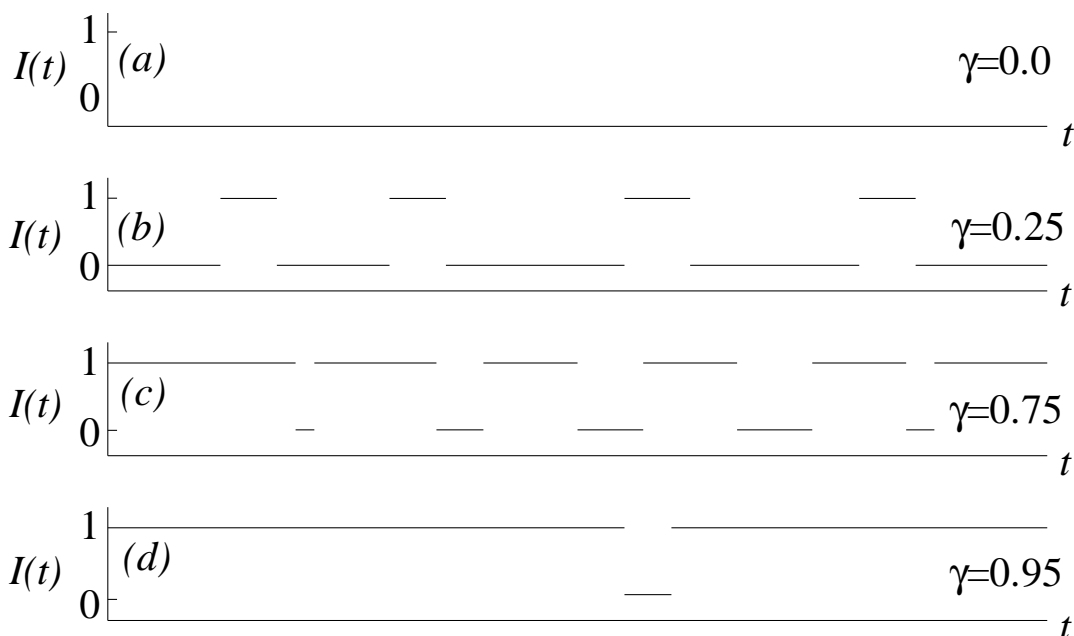


Figure 5.39: Sketch of the intermittency function vs. time in a free shear flow (a) in the irrotational non-turbulent surroundings (b) in the outer part of the intermittent region (c) in the inner part of the intermittent region and (d) close to the center of the flow.

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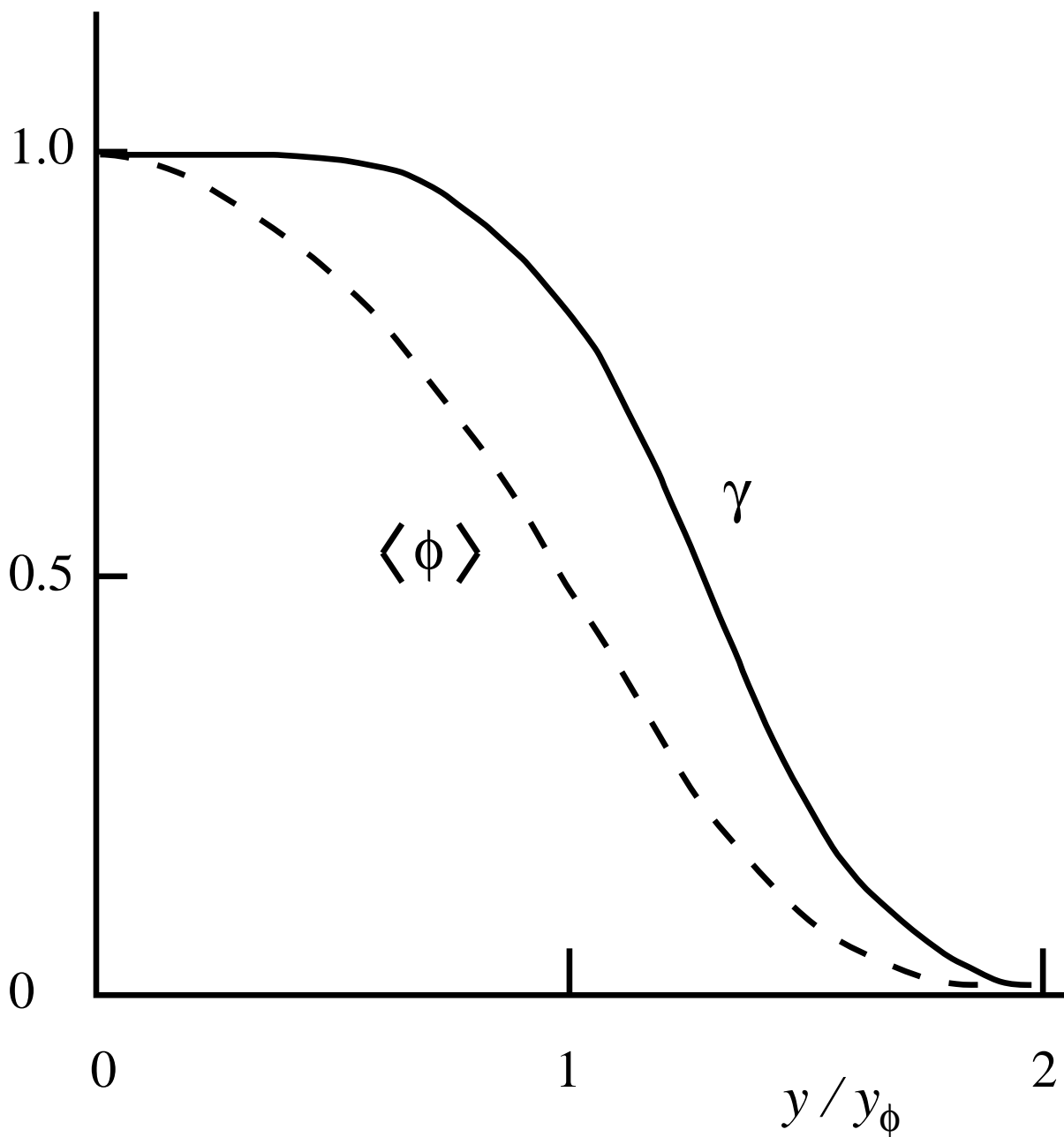


Figure 5.40: Profile of the intermittency factor in the self-similar plane wake. The mean scalar profile shown for comparison: y_ϕ is the half-width. From the experimental data of LaRue and Libby (1974, 1976).

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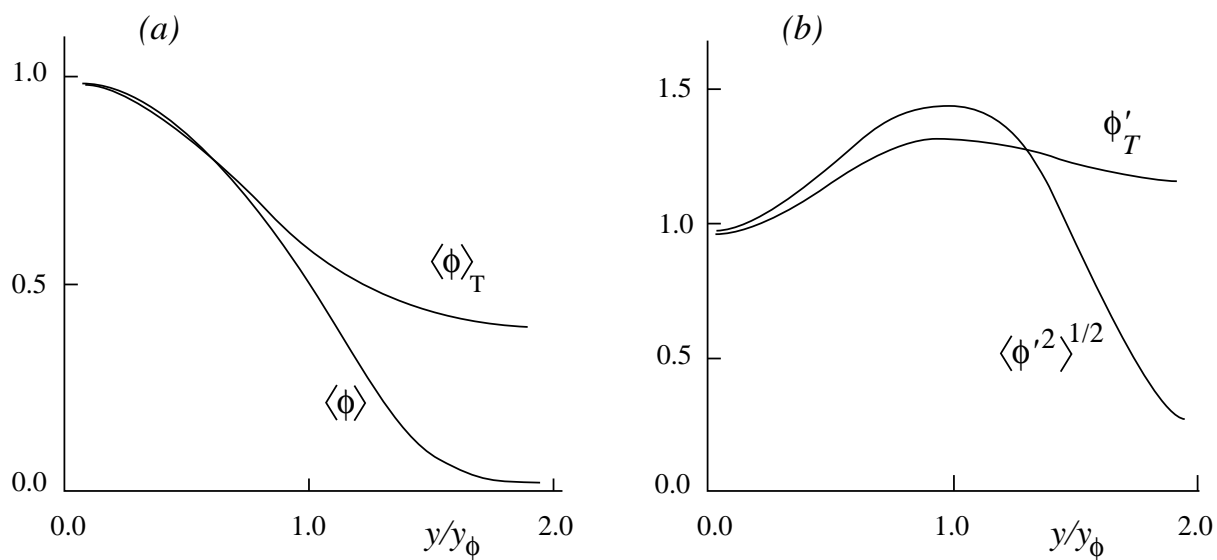


Figure 5.41: Comparison of unconditional and turbulent mean (a) and r.m.s. (b) scalar profiles in the self-similar plane wake. From the experimental data of LaRue and Libby (1974).

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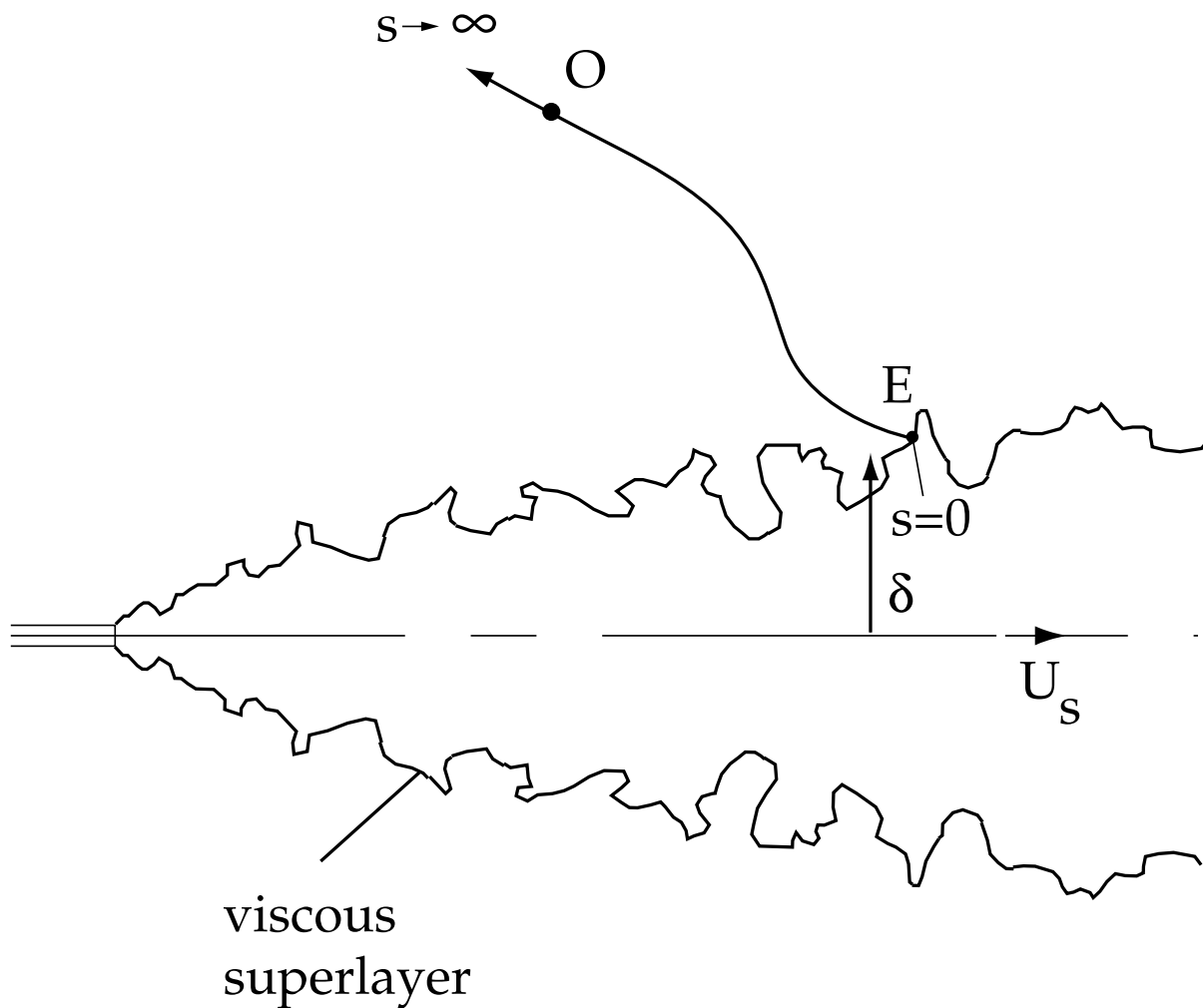


Figure 5.42: Sketch of a turbulent round jet showing the viscous superlayer, and the path of a fluid particle from a point in the quiescent ambient, O , to the superlayer, E .

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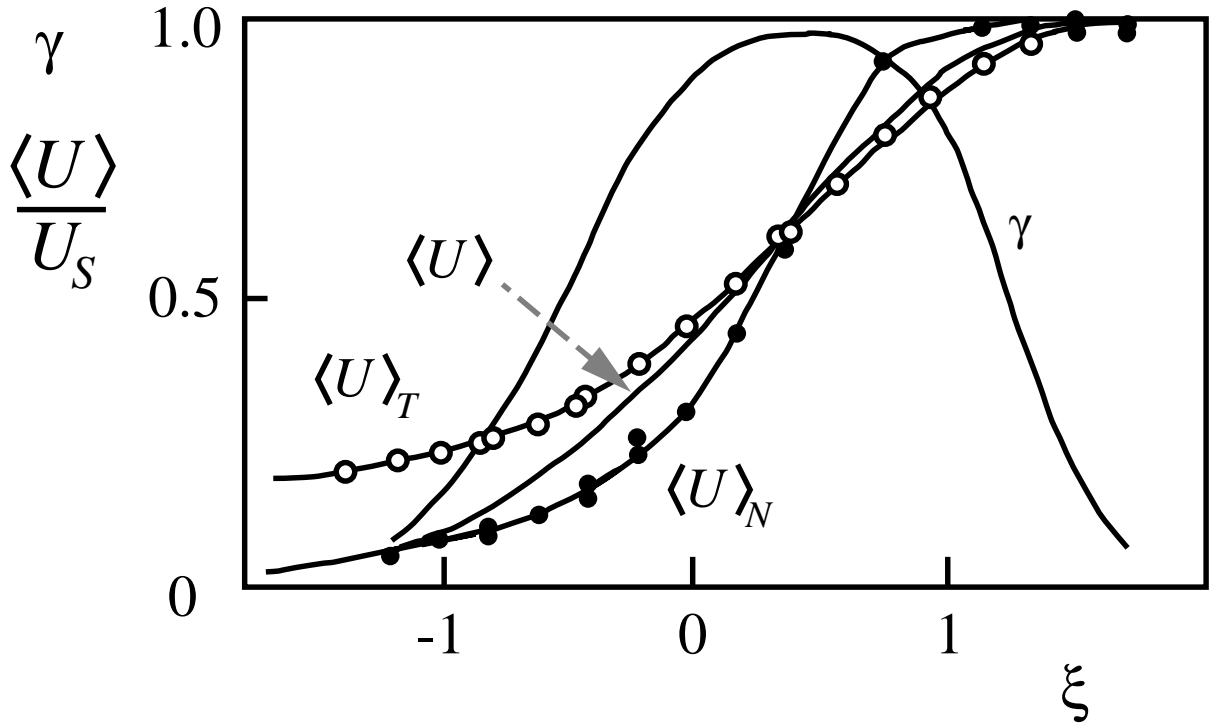


Figure 5.43: Profiles of the intermittency factor γ , the unconditional mean axial velocity $\langle U \rangle$ and the turbulent $\langle U \rangle_T$ and non-turbulent $\langle U \rangle_N$ conditional mean velocities in a self-similar mixing layer. From the experimental data of Wygnanski and Fiedler (1970).

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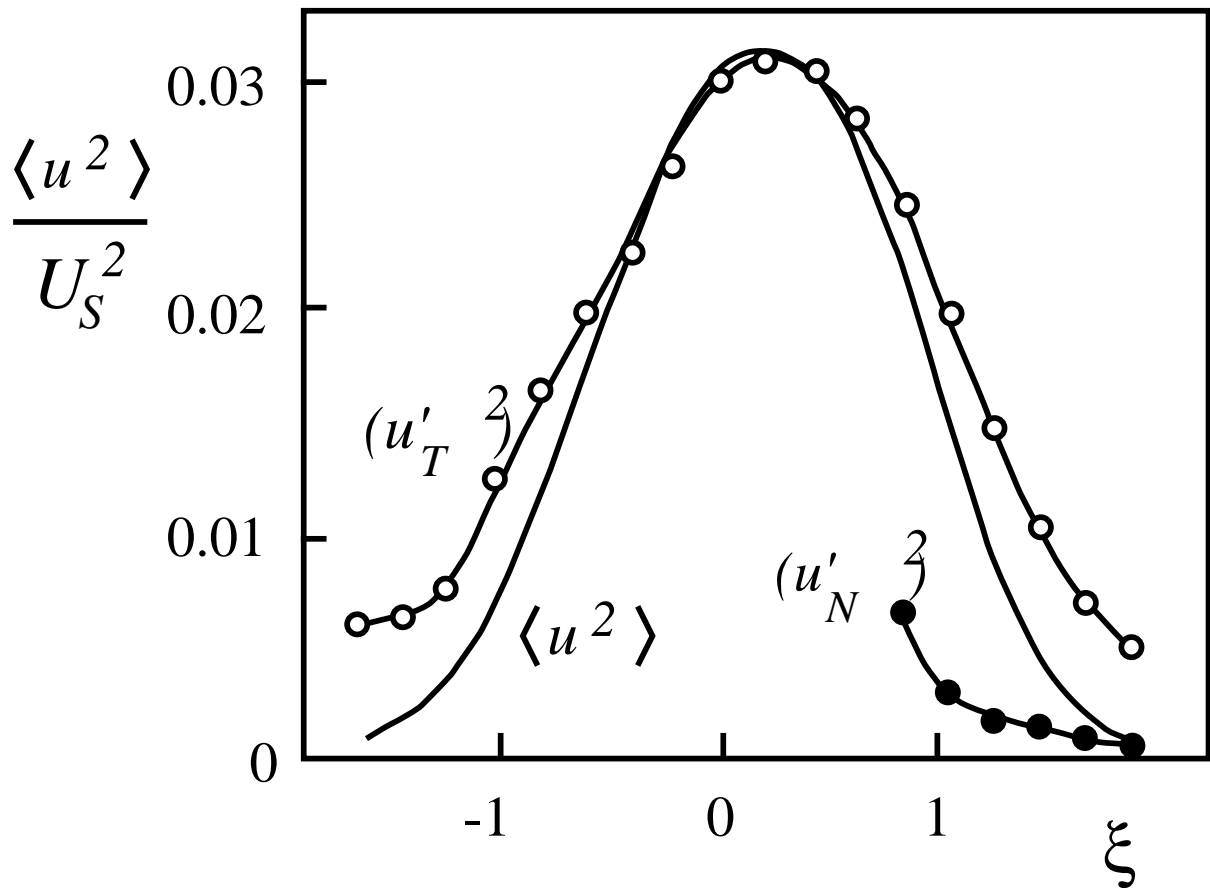


Figure 5.44: Profiles of unconditional $\langle u^2 \rangle$, turbulent $(u'_T)^2$ and non-turbulent $(u'_N)^2$ variances of axial velocity in a self-similar mixing layer. From the experimental data of Wygnanski and Fiedler (1970).

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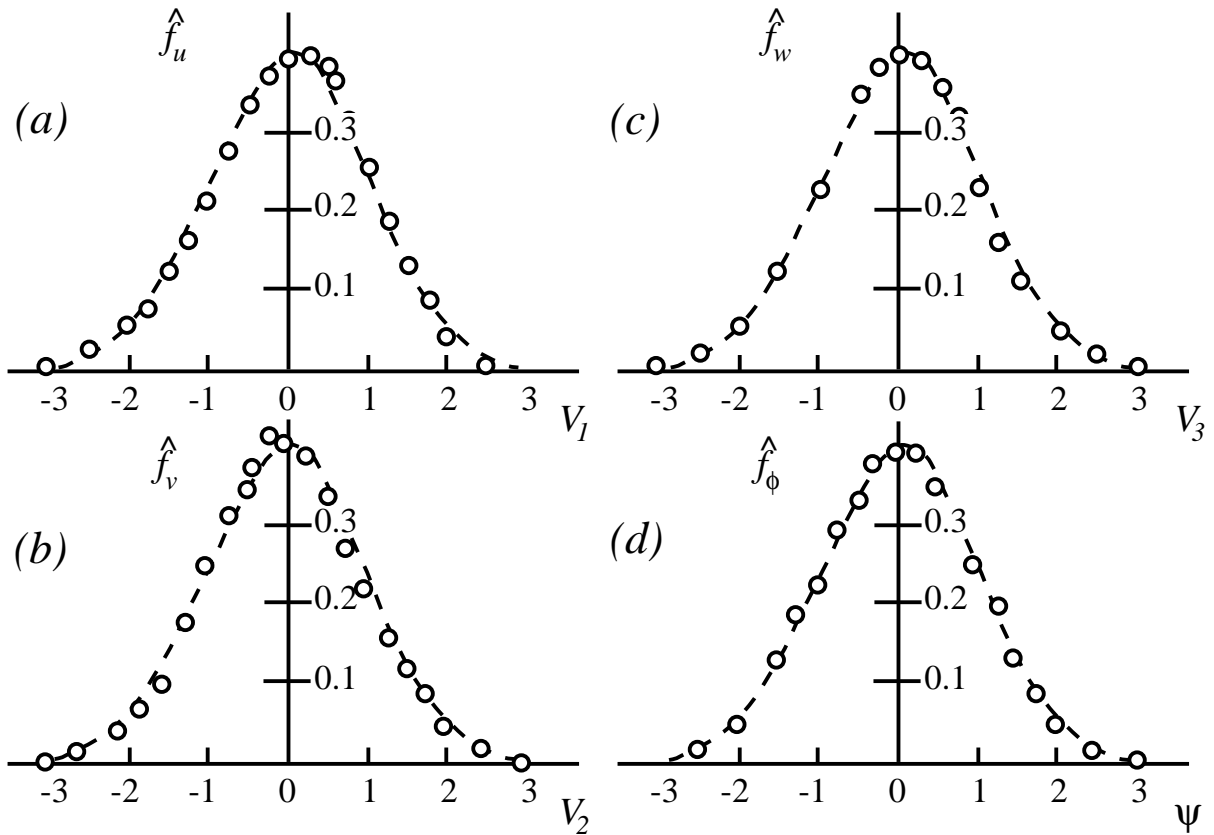


Figure 5.45: Standardized PDF's of (a) u , (b) v , (c) w and (d) ϕ in homogeneous shear flow. Dashed lines are standardized Gaussians. (From Tavoularis and Corrsin (1981).)

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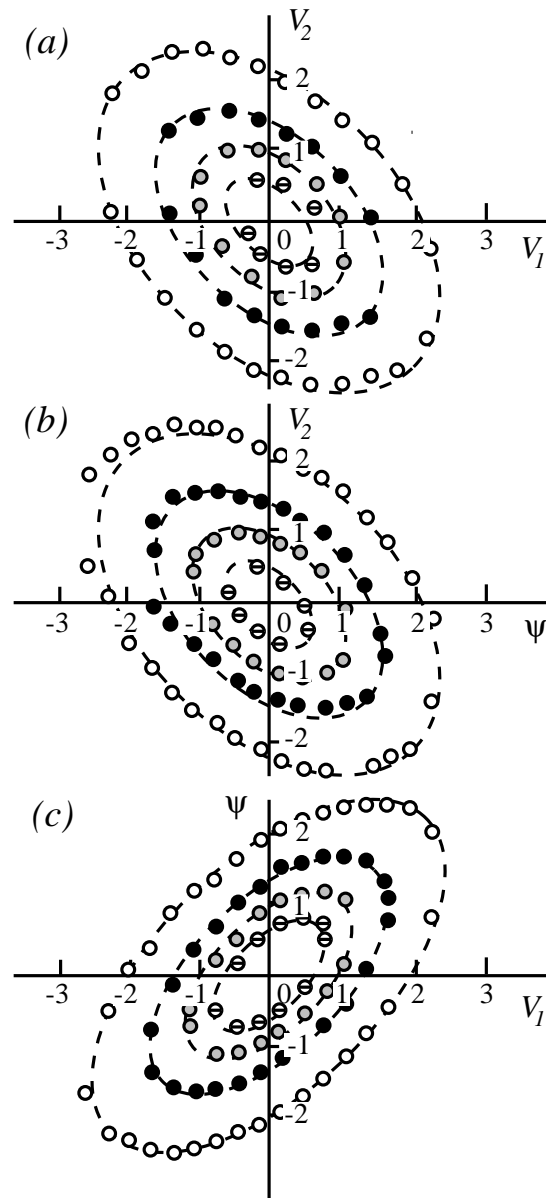


Figure 5.46: Contour plots of joint PDF's of standardized variables measured in homogeneous shear flow: (a) u and v , (b) ϕ and v , (c) u and ϕ . Contour values are 0.15, 0.10, 0.05 and 0.01. Dashed lines are corresponding contours for joint-normal distributions with the same correlation coefficients. (From Tavoularis and Corrsin (1981).)

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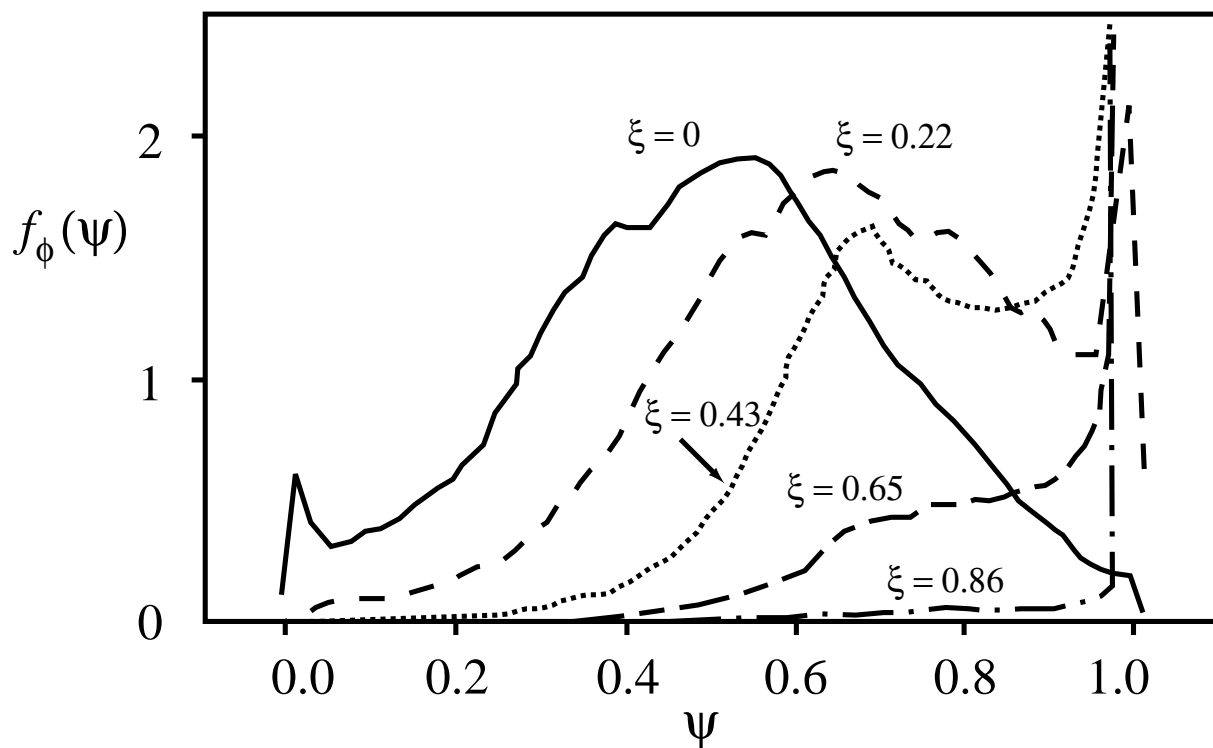


Figure 5.47: PDF's of a conserved passive scalar in the self-similar temporal mixing layer at different lateral positions. From direct numerical simulations of Rogers and Moser (1994).

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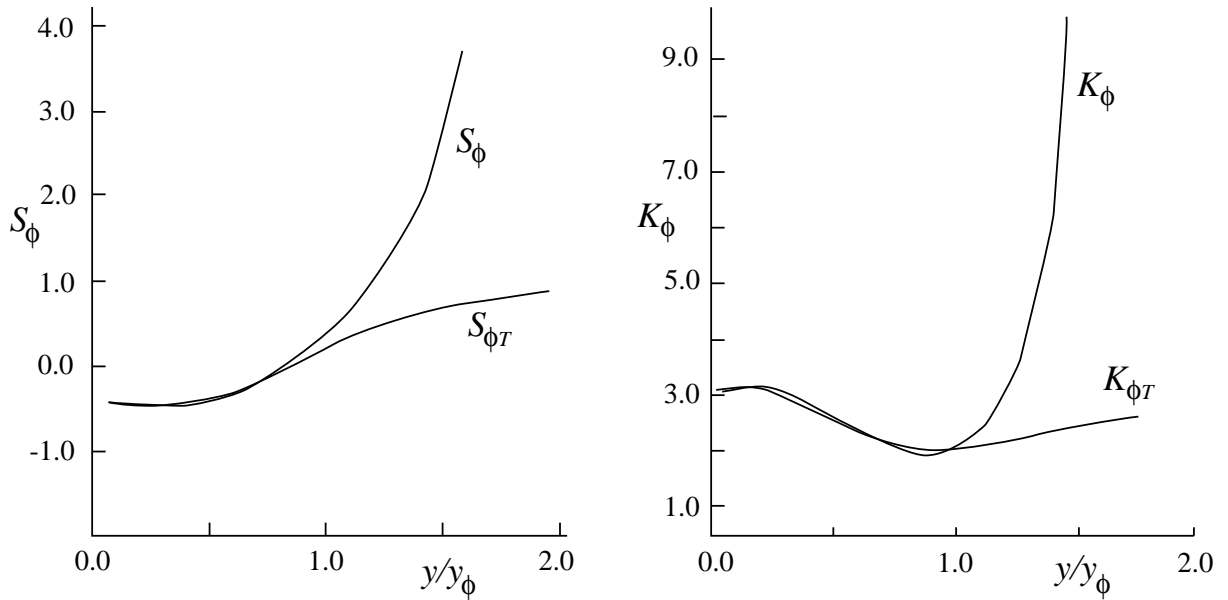


Figure 5.48: Profiles of unconditional (S_ϕ, K_ϕ) and conditional turbulent ($S_{\phi T}, K_{\phi T}$) skewness and kurtosis of a conserved passive scalar in the self-similar plane wake. From the experimental data of LaRue and Libby (1974).

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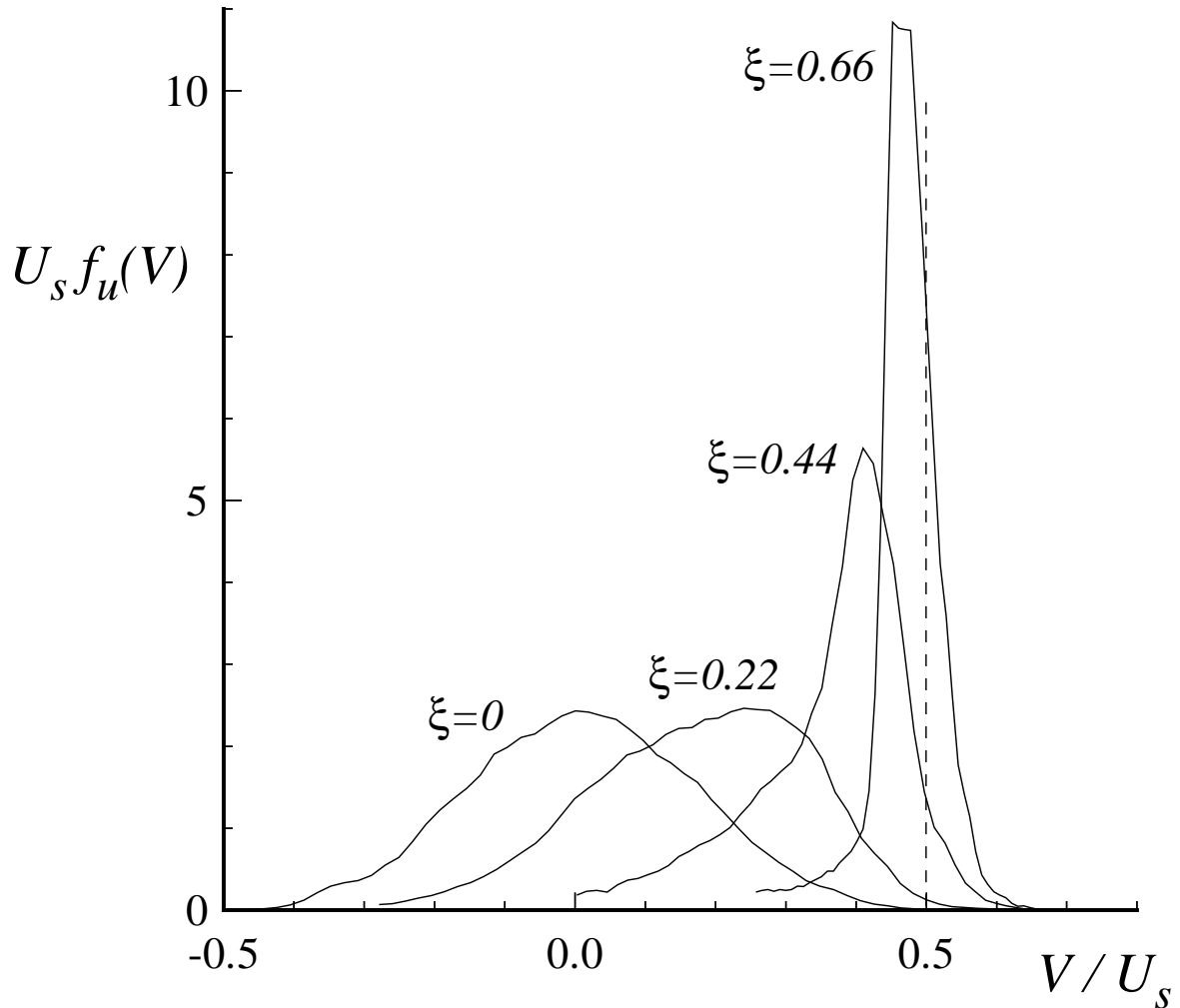


Figure 5.49: PDF's of axial velocity in a temporal mixing layer. The distance from the center of the layer is $\xi = y/\delta$. The dashed line corresponds to the freestream velocity U_h . From the DNS data of Rogers and Moser (1994).

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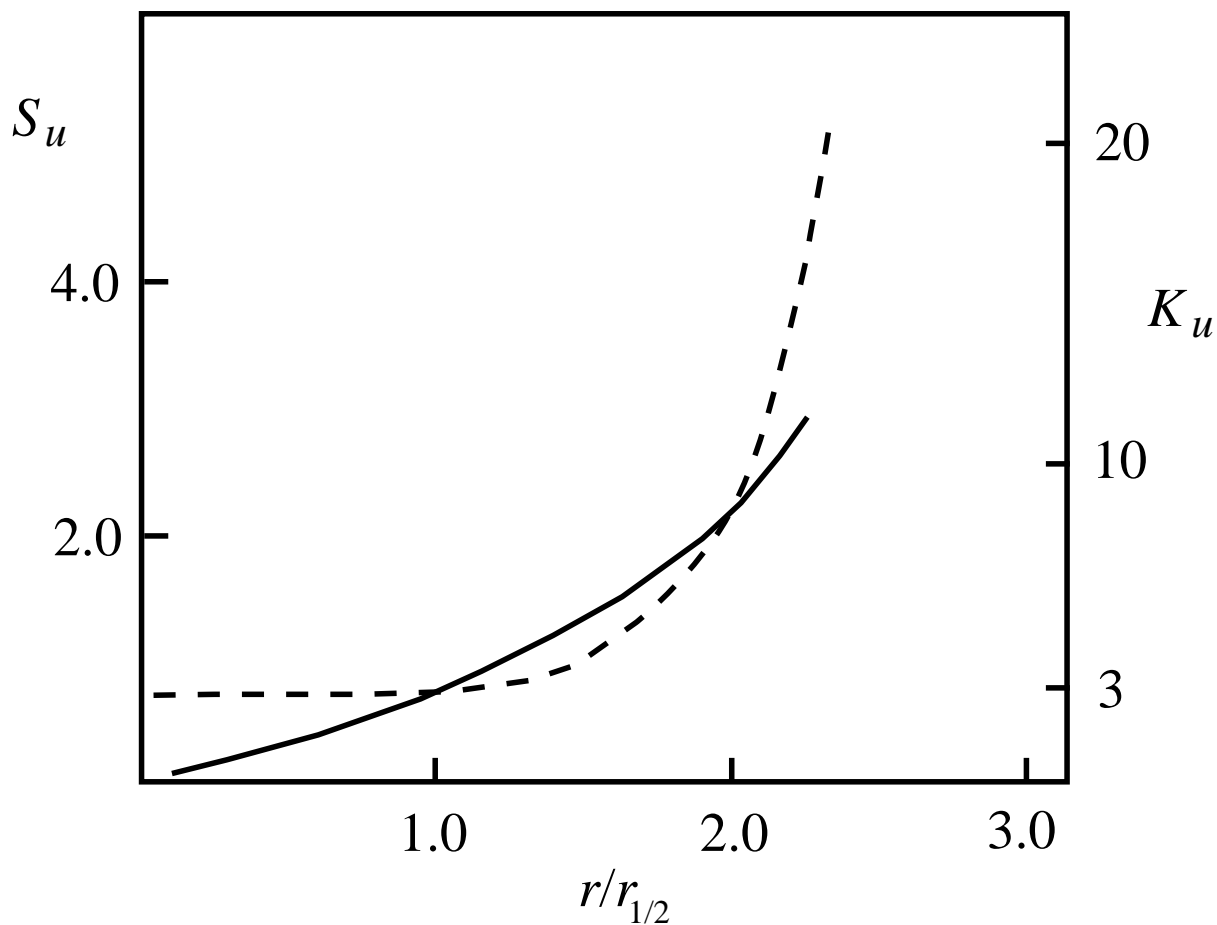


Figure 5.50: Profiles of skewness (solid line) and kurtosis (dashed line) in the self-similar round jet. From the experimental data of Wygnanski and Fiedler (1969).

CHAPTER 5: FREE SHEAR FLOWS

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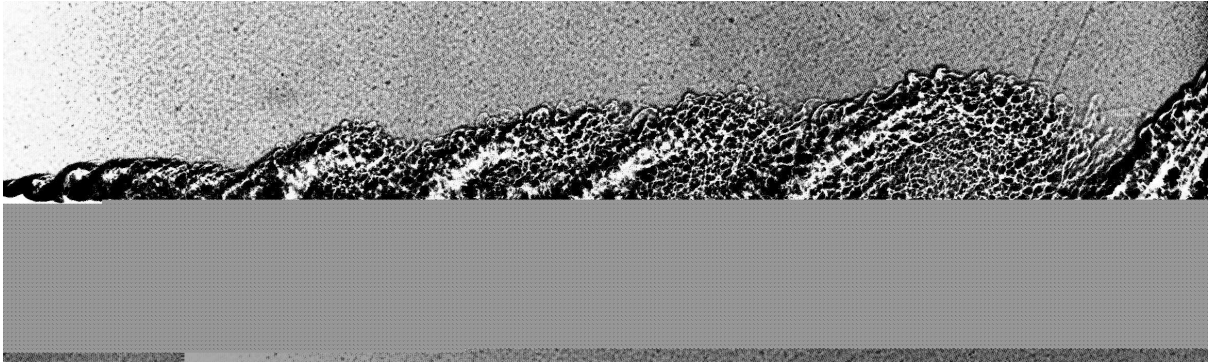


Figure 5.51: Flow visualization of a plane mixing layer. Spark shadow graph of a mixing layer between helium (upper) $U_h = 10.1m/s$ and nitrogen (lower) $U_\ell = 3.8m/s$ at a pressure of 8 atm. (From Brown and Roshko (1974).)

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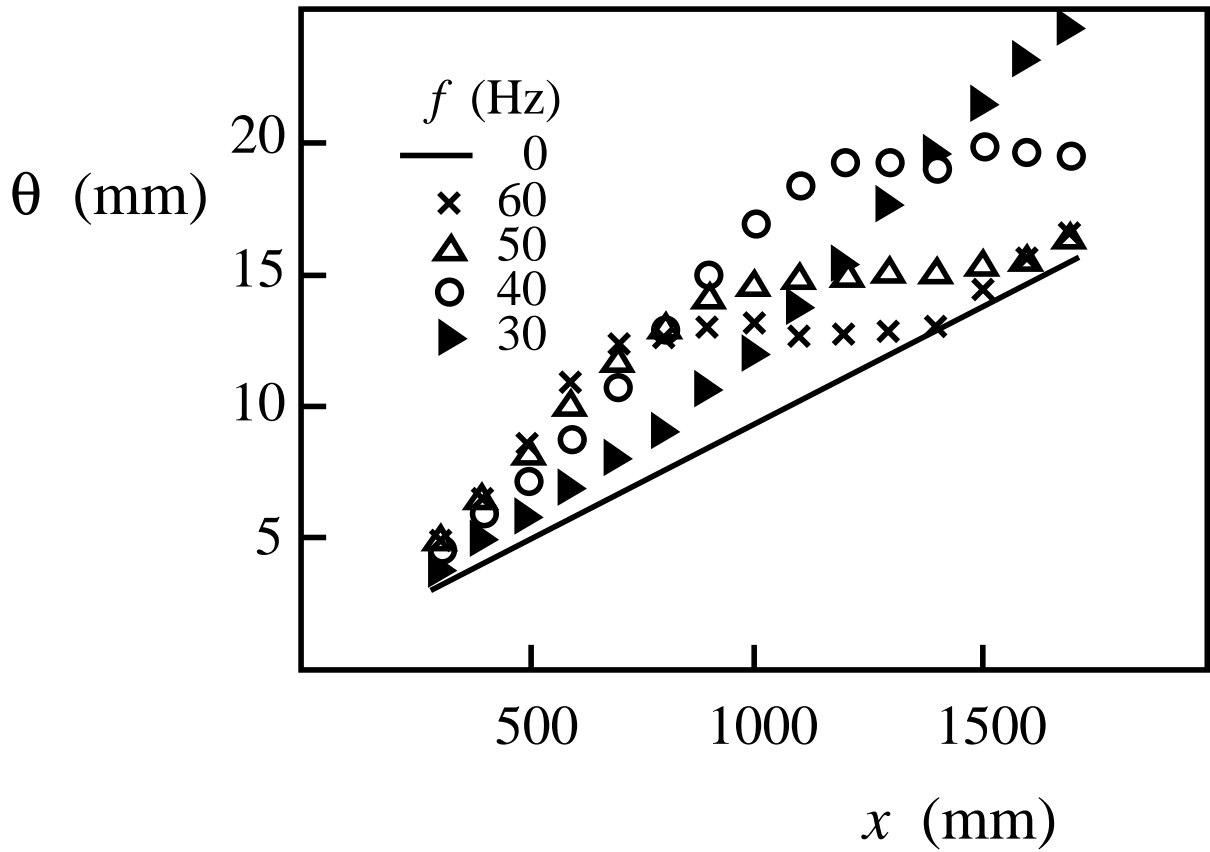


Figure 5.53: Mixing layer thickness, θ , against axial distance, x , for different forcing frequencies, f . (From Oster and Wygnanski (1982).)